# Survivable composite-link IP network design with OSPF routing

Talk given at
Eighth INFORMS Telecommunications Conference
Dallas, Texas
April 1, 2006



Mauricio G. C. Resende

AT&T Labs Research
Florham Park, New Jersey
mgcr@research.att.com
www.research.att.com/~mgcr

Joint work with D.V. Andrade, L.S. Buriol & M. Thorup

- OSPF routing
- Survivable IP network design
- Composite-link design
- Concluding remarks



- OSPF routing
- Survivable IP network design
- Composite-link design
- Concluding remarks



- OSPF routing
- Survivable IP network design
- Composite-link design
- Concluding remarks



- OSPF routing
- Survivable IP network design
- Composite-link design
- Concluding remarks



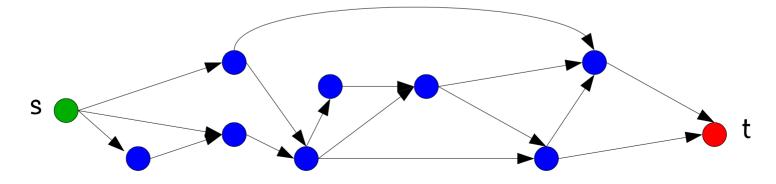
• Given a network G = (N,A), where N is the set of routers and A is the set of links.



- Given a network G = (N,A), where N is the set of routers and A is the set of links.
- The OSPF (open shortest path first) routing protocol assumes each link a has a weight w(a) assigned to it so that a packet from a source router s to a destination router t is routed on a shortest weight path from s to t.

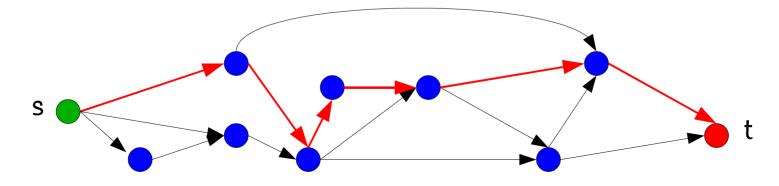


- Given a network G = (N,A), where N is the set of routers and A is the set of links.
- The OSPF (open shortest path first) routing protocol assumes each link a has a weight w(a) assigned to it so that a packet from a source router s to a destination router t is routed on a shortest weight path from s to t.



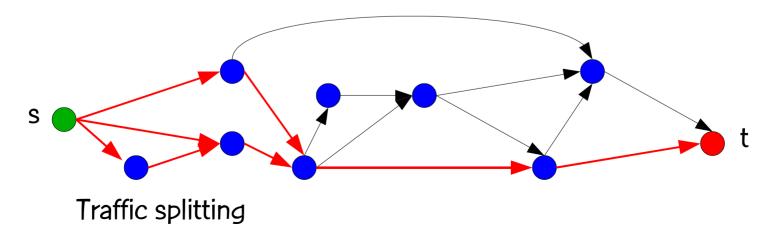


- Given a network G = (N,A), where N is the set of routers and A is the set of links.
- The OSPF (open shortest path first) routing protocol assumes each link a has a weight w(a) assigned to it so that a packet from a source router s to a destination router t is routed on a shortest weight path from s to t.





- Given a network G = (N,A), where N is the set of routers and A is the set of links.
- The OSPF (open shortest path first) routing protocol assumes each link a has a weight w(a) assigned to it so that a packet from a source router s to a destination router t is routed on a shortest weight path from s to t.





- By setting OSPF weights appropriately, one can do traffic engineering, i.e. route traffic so as to optimize some objective (e.g. minimize congestion, maximize throughput, etc.).
- Some recent papers on this topic:
  - Fortz & Thorup (2000, 2004)
  - Ramakrishnan & Rodrigues (2001)
  - Sridharan, Guérin, & Diot (2002)
  - Fortz, Rexford, & Thorup (2002)
  - Ericsson, Resende, & Pardalos (2002)
  - Buriol, Resende, Ribeiro, & Thorup (2002, 2005)



- By setting OSPF weights appropriately, one can do traffic engineering, i.e. route traffic so as to optimize some objective (e.g. minimize congestion, maximize throughput, etc.).
- Some recent papers on this topic:
  - Fortz & Thorup (2000, 2004)
  - Ramakrishnan & Rodrigues (2001)
  - Sridharan, Guérin, & Diot (2002)
  - Fortz, Rexford, & Thorup (2002)
  - Ericsson, Resende, & Pardalos (2002)
  - Buriol, Resende, Ribeiro, & Thorup (2002, 2005)



 Buriol, Resende, and Thorup (Networks, 2006) use weight setting to design survivable IP networks.



 Buriol, Resende, and Thorup (Networks, 2006) use weight setting to design survivable IP networks.

#### Given

- directed graph G = (N,A), where N is the set of routers, A is the set of potential arcs where capacity can be installed,
- a demand matrix D that for each pair  $(s,t) \in N \times N$ , specifies the demand D(s,t) between s and t,
- a cost K(a) to lay fiber on arc a
- a capacity increment C for the fiber.



 Buriol, Resende, and Thorup (Networks, 2006) use weight setting to design survivable IP networks.

#### Determine

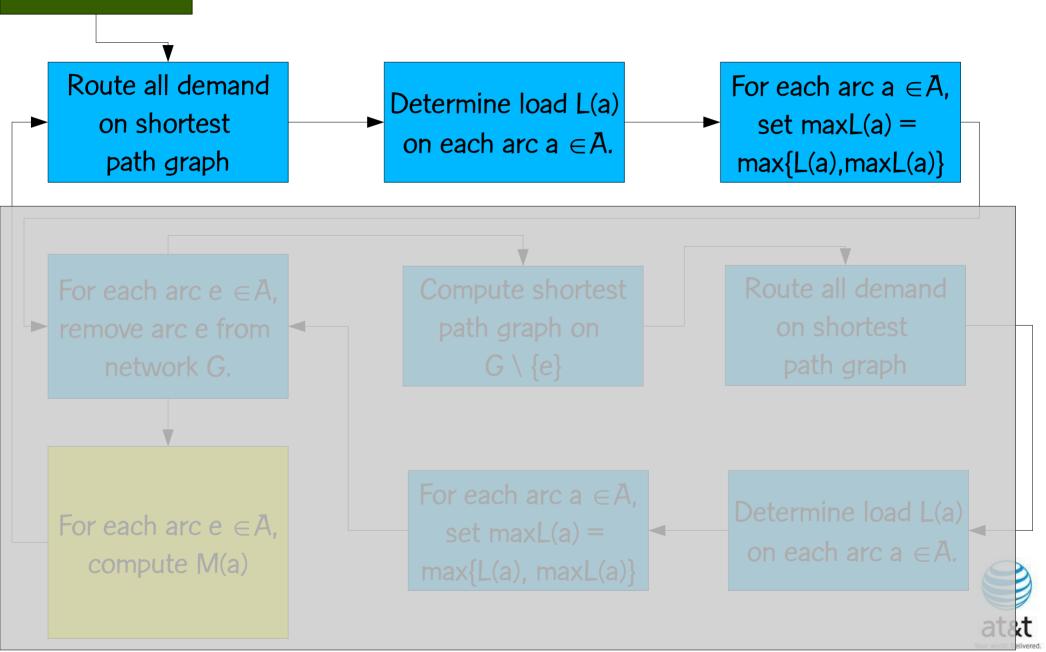
- OSPF weight w(a) to assign to each arc  $a \in A$ ,
- which arcs should be used to deploy fiber and how many units (multiplicities) M(a) of capacity C should be installed on each arc a ∈ A,
- such that all the demand can be routed on the network even when any single arc fails.
- Minimize total design cost =  $\sum_{a \in A} M(a) \times K(a)$ .



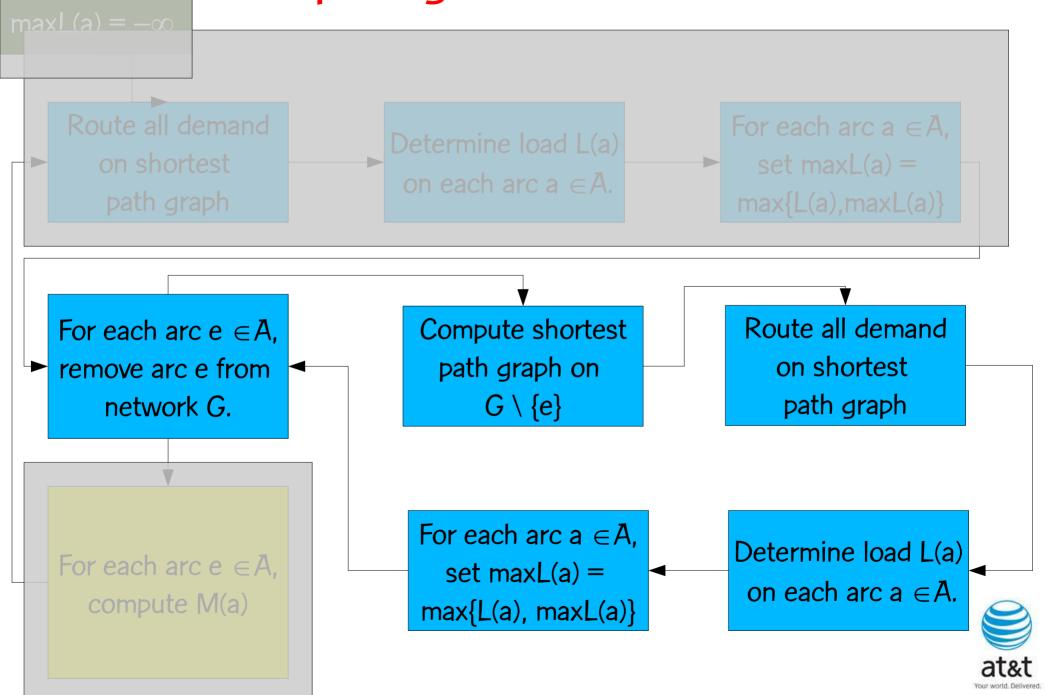
- Buriol, Resende, and Thorup (Networks, 2006) use weight setting to design survivable IP networks.
- Use genetic algorithm (GA) to determine weights.
- GA needs to compute "fitness" of each solution it produces.



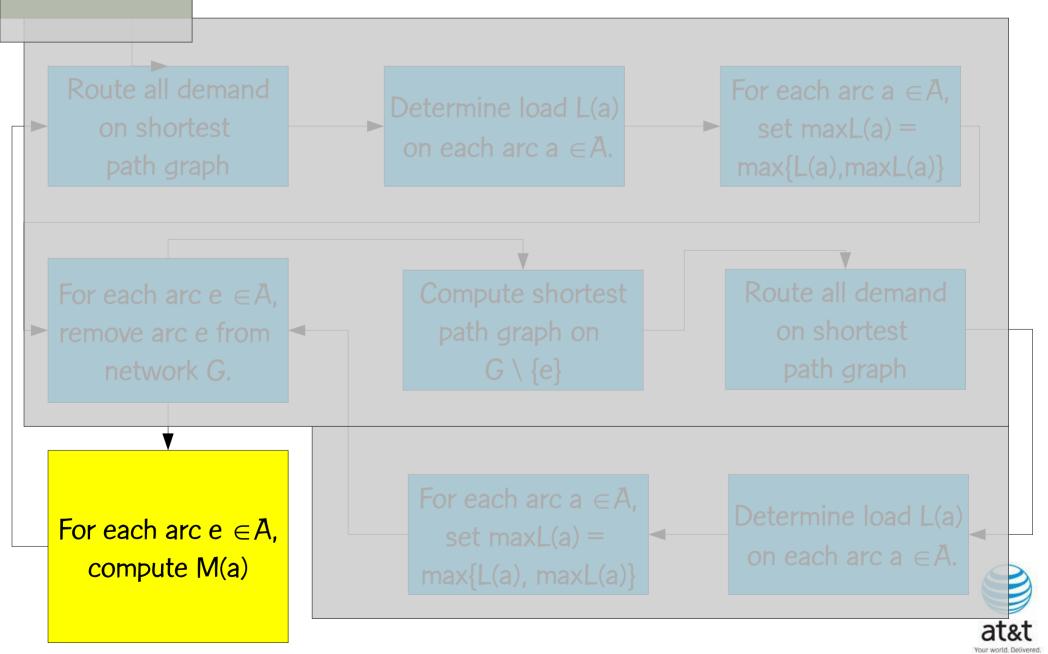
For each arc  $a \in A$ , set  $\max L(a) = -\infty$ 



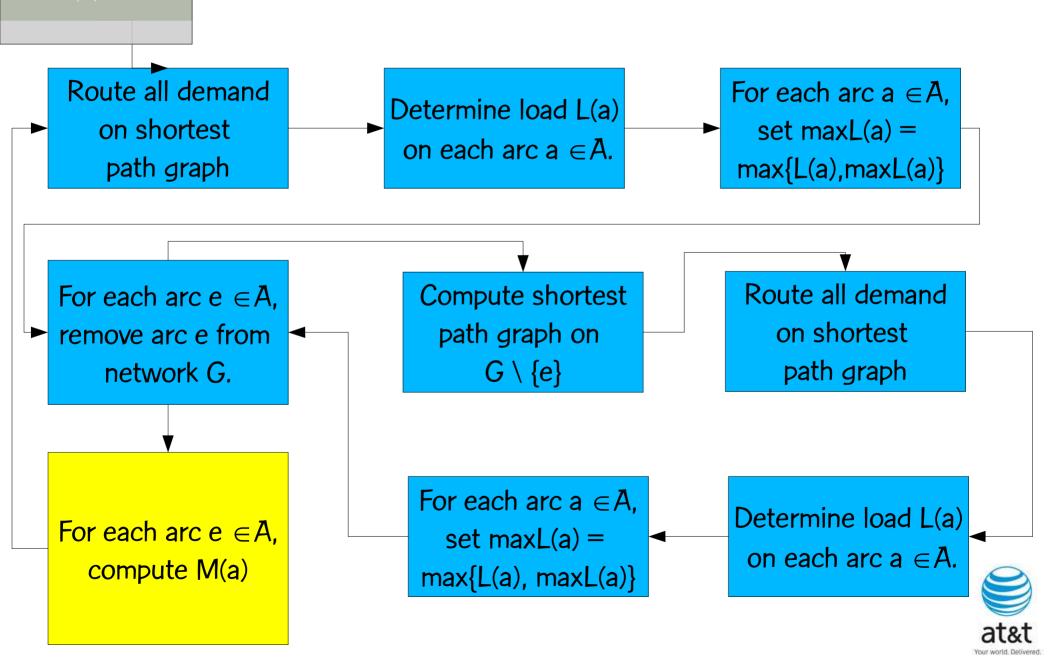
For each arc  $a \in A$ , set  $\max (a) = -\infty$ 



For each arc  $a \in A$ , set  $\max L(a) = -\infty$ 



For each arc  $a \in A$ , set  $\max L(a) = -\infty$ 



- In Buriol, Resende, and Thorup (2006)
  - links were all of the same type,
  - only the link multiplicity had to be determined.
- Now consider composite links. Given a load L(a) on arc a, we can compose several different link types that sum up to the needed capacity  $c(a) \ge L(a)$ :

$$-c(a) = \sum_{\text{t used in arc a}} M(t) \times \gamma(t)$$
, where

- M(t) is the multiplicity of link type t
- $-\gamma(t)$  is the capacity of link type t



- In Buriol, Resende, and Thorup (2006)
  - links were all of the same type,
  - only the link multiplicity had to be determined.
- Now consider composite links. Given a load L(a) on arc a, we can compose several different link types that sum up to the needed capacity  $c(a) \ge L(a)$ :
  - $-c(a) = \sum_{\text{t used in arc a}} M(t) \times \gamma(t)$ , where
  - M(t) is the multiplicity of link type t
  - $-\gamma(t)$  is the capacity of link type t



- Link types = { 1, 2, ..., T }
- Capacities =  $\{c(1), c(2), ..., c(T)\}: c(i) < c(i+1)$
- Prices / unit length = { p(1), p(2), ..., p(T) }: p(i) < p(i+1)
- Assumptions:
  - $[p(T)/c(T)] < [p(T-1)/c(T-1)] < \cdots < [p(1)/c(1)]$ , i.e. price per unit of capacity is smaller for links with greater capacity
  - $c(i) = \alpha \times c(i-1)$ , for  $\alpha \in \mathbb{N}$ ,  $\alpha > 1$ , i.e. capacities are multiples of each other by powers of  $\alpha$



- Link types = { 1, 2, ..., T }
- Capacities =  $\{c(1), c(2), ..., c(T)\}: c(i) < c(i+1)$
- Prices / unit length = { p(1), p(2), ..., p(T) }: p(i) < p(i+1)
- Assumptions:
  - $[p(T)/c(T)] < [p(T-1)/c(T-1)] < \cdots < [p(1)/c(1)]$ , i.e. price per unit of capacity is smaller for links with greater capacity
  - $c(i) = \alpha \times c(i-1)$ , for  $\alpha \in \mathbb{N}$ ,  $\alpha > 1$ , i.e. capacities are multiples of each other by powers of  $\alpha$



- Link types = { 1, 2, ..., T }
- Capacities =  $\{c(1), c(2), ..., c(T)\}: c(i) < c(i+1)$
- Prices / unit length = { p(1), p(2), ..., p(T) }: p(i) < p(i+1)
- Assumptions:
  - $[p(T)/c(T)] < [p(T-1)/c(T-1)] < \cdots < [p(1)/c(1)]$ : economies of scale
  - $c(i) = \alpha \times c(i-1)$ , for  $\alpha \in \mathbb{N}$ ,  $\alpha > 1$ , e.g.  $c(OC192) = 4 \times c(OC48)$ ;  $c(OC48) = 4 \times c(OC12)$ ;  $c(OC12) = 4 \times c(OC3)$ ;

OC3	OC12	OC48	OC192	
155 Mb/s	622 Mb/s	2.5 Gb/s	10 Gb/s	$\alpha = 4$



- Designed to minimize overall network cost.
- Heuristics are:
  - Min capacity
  - Min cost
  - Min cost k types
  - Min multiplicities



- Designed to minimize overall network cost.
- Heuristics are:
  - Min capacity
  - Min cost
  - Min cost k types
  - Min multiplicities



- Designed to minimize overall network cost.
- Heuristics are:
  - Min capacity
  - Min cost
  - Min cost k types
  - Min multiplicities



- Designed to minimize overall network cost.
- Heuristics are:
  - Min capacity
  - Min cost
  - Min cost k types
  - Min multiplicities



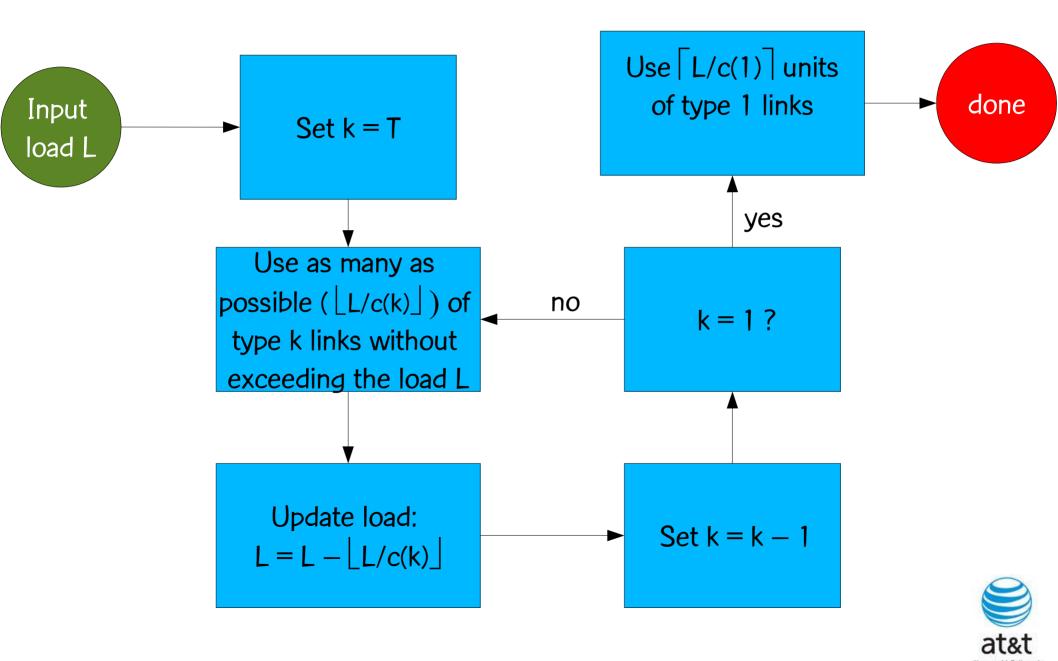
- Designed to minimize overall network cost.
- Heuristics are:
  - Min capacity
  - Min cost
  - Min cost k types
  - Min multiplicities

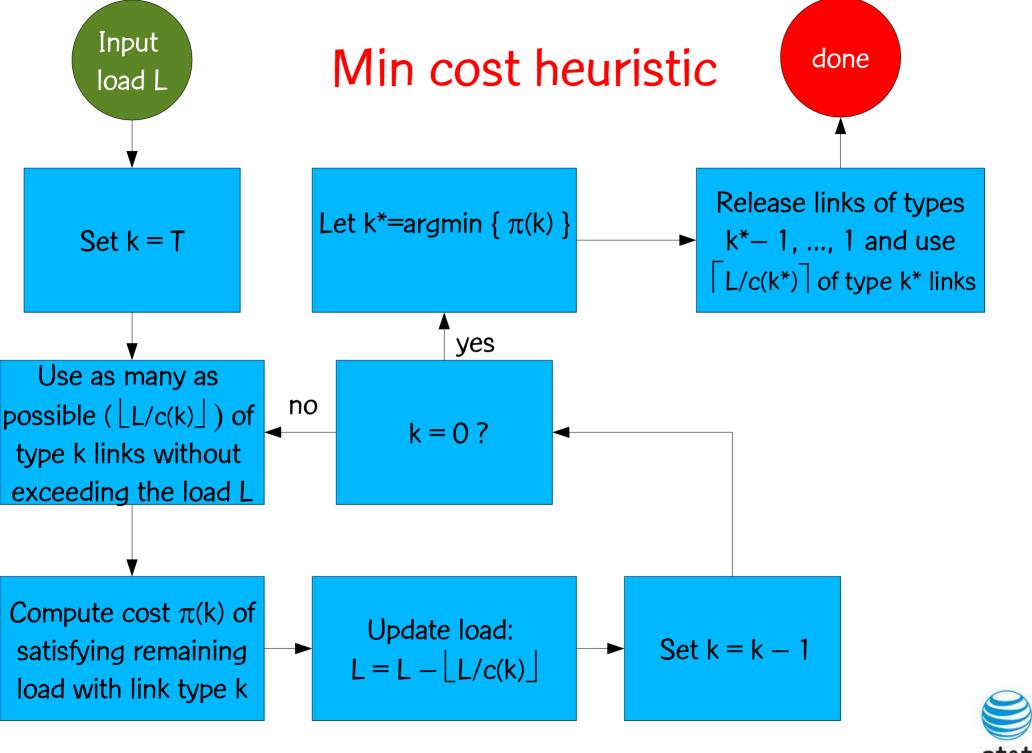


- Designed to minimize overall network cost.
- Heuristics are:
  - Min capacity
  - Min cost
  - Min cost k types
  - Min multiplicities



# Min capacity heuristic





 $\pi(k)$  is total cost of using links of types T, T– 1, ..., k.

#### Min cost k types

- Follows same idea as "Min cost" heuristic.
- Can use at most k different link types.
- In some applications, this additional constraint can be imposed.
- Use small values of k, e.g. k=1, k=2



#### Min cost k types

- Follows same idea as "Min cost" heuristic.
- Can use at most k different link types.
- In some applications, this additional constraint can be imposed.
- Use small values of k, e.g. k=1, k=2



#### Min cost k types

- Follows same idea as "Min cost" heuristic.
- Can use at most k different link types.
- In some applications, this additional constraint can be imposed.
- Use small values of k, e.g. k=1, k=2



- Follows same idea as "Min cost" heuristic.
- Can use at most k different link types.
- In some applications, this additional constraint can be imposed.
- Use small values of k, e.g. k=1, k=2



- Let L be the load on the arc.
- For each link type  $k \in \{1, 2, ..., T\}$  compute cost  $\pi(k)$  of deploying  $\lceil L/c(k) \rceil$  units of link type k.
- Let  $k^*$ =argmin {  $\pi(k)$ :  $k \in \{1, 2, ..., T\}$  } be the least cost link type.
- Deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ .



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k)
   of deploying L/c(k) units of link type k.
- Let  $k^*$ =argmin {  $\pi(k)$ :  $k \in \{1, 2, ..., T\}$  } be the least cost link type.
- Deploy L/c(k\*) units of link type k\*.



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k)
   of deploying L/c(k) units of link type k.
- Let  $k^*=argmin \{ \pi(k): k \in \{ 1, 2, ..., T \} \}$  be the least cost link type.
- Deploy \[ \( \( \) \\ \) units of link type k\*.



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k)
  of deploying \[ L/c(k) \] units of link type k.
- Let  $k^*=argmin \{ \pi(k): k \in \{ 1, 2, ..., T \} \}$  be the least cost link type.
- Deploy \[ \textsup L/c(k\*) \] units of link type k\*.



- Let L be the load on the arc.
- For each link type  $k \in \{1, 2, ..., T\}$  compute cost  $\pi(k)$  of deploying  $\lceil L/c(k) \rceil$  units of link type k.
- For each pair of link types i and j (j > i) compute cost  $\Pi(i,j)$  of deploying  $\lfloor L/c(j) \rfloor$  units of link type j and  $\lceil L/c(i) \rceil$  units of link type i.
- Let  $k^*$ =argmin {  $\pi(k)$  } and  $(i^*,j^*)$  = argmin {  $\Pi(i,j)$  }.
- If  $\Pi(i^*,j^*) > \pi(k^*)$  deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ ;
- Else deploy L/c(j\*) units of link type j\* and L/c(i\*) units of link type i\*.



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k) of deploying \[ L/c(k) \] units of link type k.
- For each pair of link types i and j (j > i) compute cost  $\Pi(i,j)$  of deploying  $\lfloor L/c(j) \rfloor$  units of link type j and  $\lceil L/c(i) \rceil$  units of link type i.
- Let  $k^*$ =argmin {  $\pi(k)$  } and  $(i^*,j^*)$  = argmin {  $\Pi(i,j)$  }.
- If  $\Pi(i^*,j^*) > \pi(k^*)$  deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ ;
- Else deploy L/c(j\*) units of link type j\* and L/c(i\*) units of link type i\*.



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k) of deploying \[ L/c(k) \] units of link type k.
- For each pair of link types i and j (j > i) compute cost  $\Pi(i,j)$  of deploying  $\lfloor L/c(j) \rfloor$  units of link type j and  $\lceil L/c(i) \rceil$  units of link type i.
- Let  $k^*$ =argmin {  $\pi(k)$  } and  $(i^*,j^*)$  = argmin {  $\Pi(i,j)$  }.
- If  $\Pi(i^*,j^*) > \pi(k^*)$  deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ ;
- Else deploy L/c(j\*) units of link type j\* and L/c(i\*) units of link type i\*.



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k) of deploying \[ L/c(k) \] units of link type k.
- For each pair of link types i and j (j > i) compute cost  $\Pi(i,j)$  of deploying  $\lfloor L/c(j) \rfloor$  units of link type j and  $\lceil L/c(i) \rceil$  units of link type i.
- Let k\*=argmin {  $\pi(k)$  } and (i\*,j\*) = argmin {  $\Pi(i,j)$  }.
- If  $\Pi(i^*,j^*) > \pi(k^*)$  deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ ;
- Else deploy L/c(j\*) units of link type j\* and L/c(i\*) units of link type i\*.



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k) of deploying \[ L/c(k) \] units of link type k.
- For each pair of link types i and j (j > i) compute cost  $\Pi(i,j)$  of deploying  $\lfloor L/c(j) \rfloor$  units of link type j and  $\lceil L/c(i) \rceil$  units of link type i.
- Let  $k^*$ =argmin {  $\pi(k)$  } and  $(i^*,j^*)$  = argmin {  $\Pi(i,j)$  }.
- If  $\Pi(i^*,j^*) > \pi(k^*)$  deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ ;
- Else deploy  $\lfloor L/c(j^*) \rfloor$  units of link type  $j^*$  and  $\lceil L/c(i^*) \rceil$  units of link type  $i^*$ .



- Let L be the load on the arc.
- For each link type k ∈ { 1, 2, ..., T } compute cost π(k) of deploying \[ L/c(k) \] units of link type k.
- For each pair of link types i and j (j > i) compute cost  $\Pi(i,j)$  of deploying  $\lfloor L/c(j) \rfloor$  units of link type j and  $\lceil L/c(i) \rceil$  units of link type i.
- Let  $k^*$ =argmin {  $\pi(k)$  } and  $(i^*,j^*)$  = argmin {  $\Pi(i,j)$  }.
- If  $\Pi(i^*,j^*) > \pi(k^*)$  deploy  $\lceil L/c(k^*) \rceil$  units of link type  $k^*$ ;
- Else deploy \[ \L/c(j\*) \] units of link type j\* and \[ \L/c(i\*) \] units of link type i\*.



- Minimizes number of copies of links used to satisfy the load.
- Multiplicity of link type k is \[ \( \L/c(k) \) \];
- If \[ L/c(T) \] > 1, then deploy \[ L/c(T) \] units of link type T and stop;
- For k = T 1, ..., 1 do:
  - If  $\lceil L/c(k) \rceil > 1$ , then deploy  $\lceil L/c(k+1) \rceil$  units of link type k+1 and stop;



- Minimizes number of copies of links used to satisfy the load.
- Multiplicity of link type k is \[ \( \L/c(k) \] \];
- If \[ L/c(T) \] > 1, then deploy \[ L/c(T) \] units of link type T and stop;
- For k = T 1, ..., 1 do:
  - If  $\lfloor L/c(k) \rfloor > 1$ , then deploy  $\lfloor L/c(k+1) \rfloor$  units of link type k+1 and stop;



- Minimizes number of copies of links used to satisfy the load.
- Multiplicity of link type k is \[ \( \L/c(k) \) \];
- If \[ \( \L/c(T) \] > 1, then deploy \[ \L/c(T) \] units of link type T and stop;
- For k = T 1, ..., 1 do:
  - If  $\lceil L/c(k) \rceil > 1$ , then deploy  $\lceil L/c(k+1) \rceil$  units of link type k+1 and stop;



- Minimizes number of copies of links used to satisfy the load.
- Multiplicity of link type k is \[ \( \L/c(k) \];
- If \[ \( \L/c(T) \] > 1, then deploy \[ \L/c(T) \] units of link type T and stop;
- For k = T 1, ..., 1 do:
  - If  $\lceil L/c(k) \rceil > 1$ , then deploy  $\lceil L/c(k+1) \rceil$  units of link type k+1 and stop;



- Subject to the assumptions listed earlier, all heuristics (except min cost k > 1 types) can be implemented to take O(T) time to execute per arc.
- Min capacity gives optimal solution for the minimum capacity objective function.
- Min cost gives the optimal solution for the minimum cost objective function.
- Without the assumptions, a knapsack problem must be solved to find min cap and min cost solutions.



- Subject to the assumptions listed earlier, all heuristics (except min cost k > 1 types) can be implemented to take O(T) time to execute per arc.
- Min capacity gives optimal solution for the minimum capacity objective function.
- Min cost gives the optimal solution for the minimum cost objective function.
- Without the assumptions, a knapsack problem must be solved to find min cap and min cost solutions.



- Subject to the assumptions listed earlier, all heuristics (except min cost k > 1 types) can be implemented to take O(T) time to execute per arc.
- Min capacity gives optimal solution for the minimum capacity objective function.
- Min cost gives the optimal solution for the minimum cost objective function.
- Without the assumptions, a knapsack problem must be solved to find min cap and min cost solutions.



- Subject to the assumptions listed earlier, all heuristics (except min cost k > 1 types) can be implemented to take O(T) time to execute per arc.
- Min capacity gives optimal solution for the minimum capacity objective function.
- Min cost gives the optimal solution for the minimum cost objective function.
- Without the assumptions, a knapsack problem must be solved to find min cap and min cost solutions.



- Use a "real" network with 54 routers and 278 arcs.
- Three link types used: { 1, 2, 3 }
- c(2) = 4 c(1); c(3) = 16 c(1)
- p(2)/c(2) = 0.95 p(1)/c(1); p(3)/c(3) = 0.90 p(1)/c(1)
- All four heuristics tested. Min cost k types was tested for k=1 and k=2.
- GA was run 100, 200, 300, ..., 1000 generations and costs were recorded for each heuristic.



- Use a "real" network with 54 routers and 278 arcs.
- Three link types used: { 1, 2, 3 }
- c(2) = 4 c(1); c(3) = 16 c(1)
- p(2)/c(2) = 0.95 p(1)/c(1); p(3)/c(3) = 0.90 p(1)/c(1)
- All four heuristics tested. Min cost k types was tested for k=1 and k=2.
- GA was run 100, 200, 300, ..., 1000 generations and costs were recorded for each heuristic.



- Use a "real" network with 54 routers and 278 arcs.
- Three link types used: { 1, 2, 3 }
- c(2) = 4 c(1); c(3) = 16 c(1)
- p(2)/c(2) = 0.95 p(1)/c(1); p(3)/c(3) = 0.90 p(1)/c(1)
- All four heuristics tested. Min cost k types was tested for k=1 and k=2.
- GA was run 100, 200, 300, ..., 1000 generations and costs were recorded for each heuristic.



- Use a "real" network with 54 routers and 278 arcs.
- Three link types used: { 1, 2, 3 }
- c(2) = 4 c(1); c(3) = 16 c(1)
- p(2)/c(2) = 0.95 p(1)/c(1); p(3)/c(3) = 0.90 p(1)/c(1)
- All four heuristics tested. Min cost k types was tested for k=1 and k=2.
- GA was run 100, 200, 300, ..., 1000 generations and costs were recorded for each heuristic.

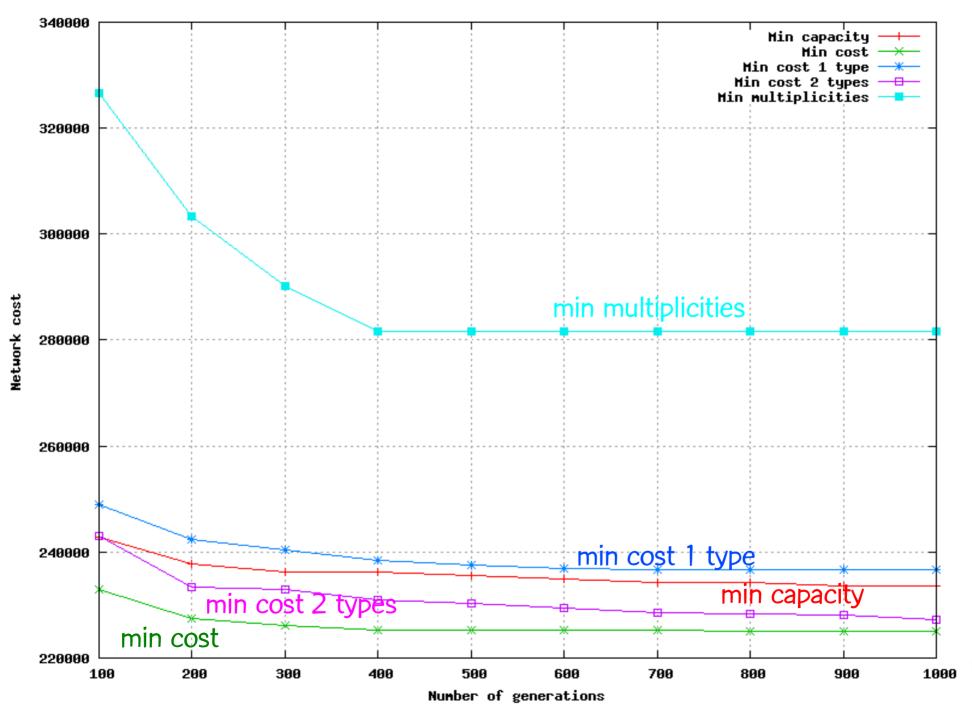


- Use a "real" network with 54 routers and 278 arcs.
- Three link types used: { 1, 2, 3 }
- c(2) = 4 c(1); c(3) = 16 c(1)
- p(2)/c(2) = 0.95 p(1)/c(1); p(3)/c(3) = 0.90 p(1)/c(1)
- All four heuristics tested. Min cost k types was tested for k=1 and k=2.
- GA was run 100, 200, 300, ..., 1000 generations and costs were recorded for each heuristic.

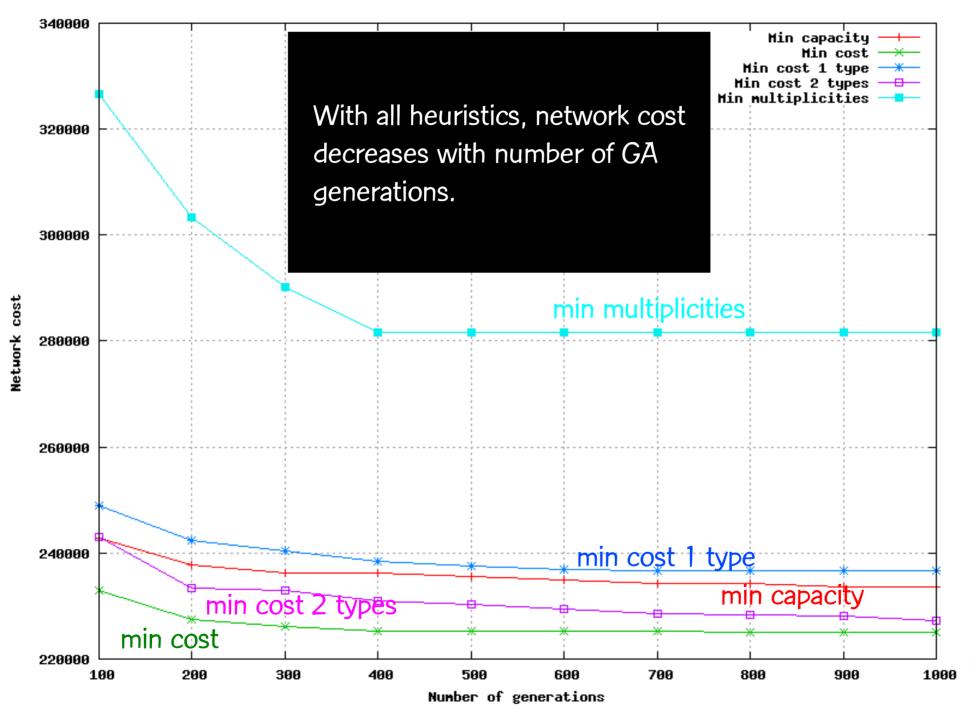


- Use a "real" network with 54 routers and 278 arcs.
- Three link types used: { 1, 2, 3 }
- c(2) = 4 c(1); c(3) = 16 c(1)
- p(2)/c(2) = 0.95 p(1)/c(1); p(3)/c(3) = 0.90 p(1)/c(1)
- All four heuristics tested. Min cost k types was tested for k=1 and k=2.
- GA was run 100, 200, 300, ..., 1000 generations and costs were recorded for each heuristic.

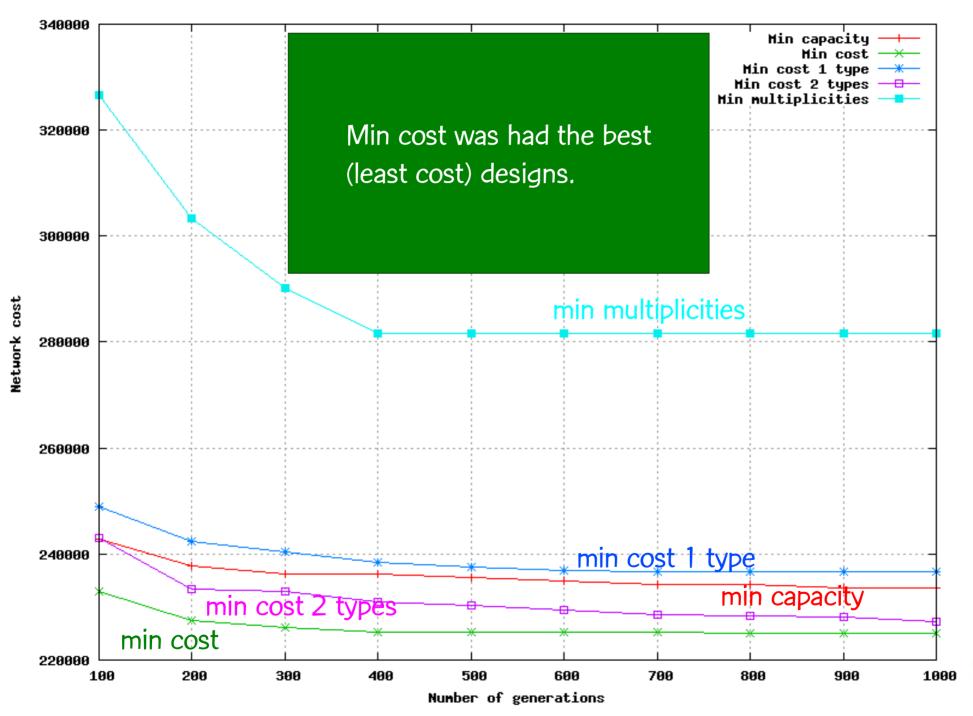




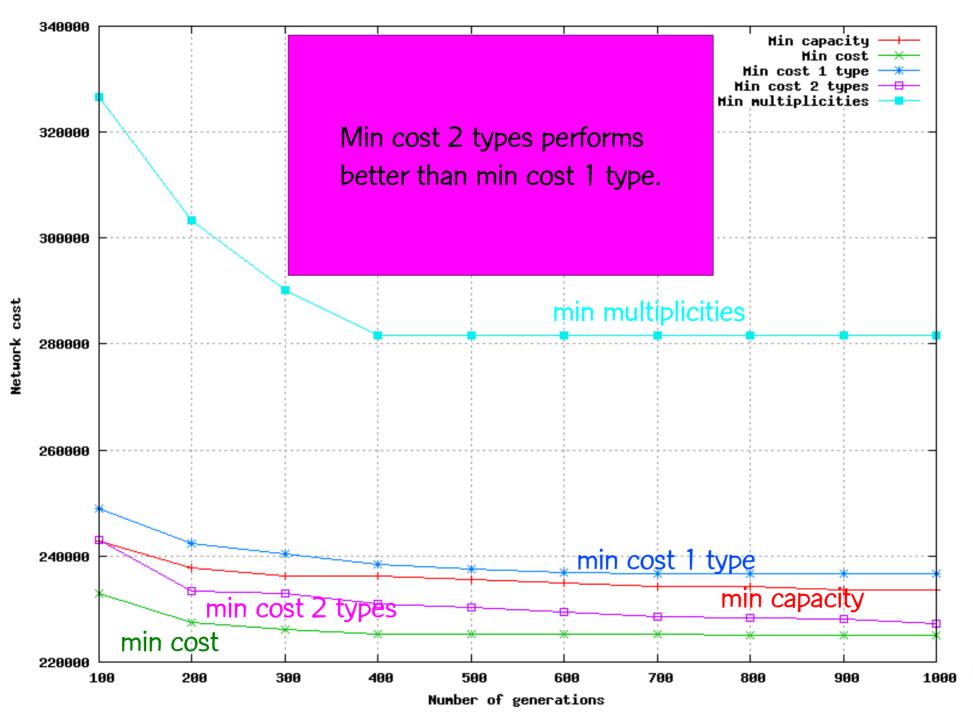




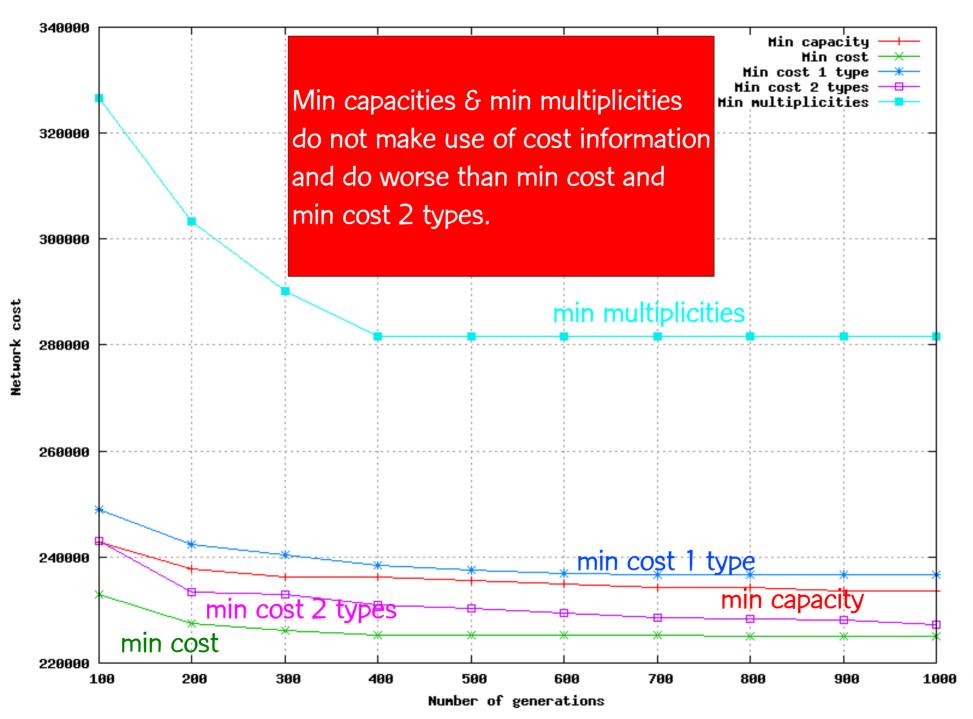














- We have extended our survivable IP network design tool to handle composite links.
- Min cost heuristic runs fast and finds best-quality solutions.
- In this talk, traffic splitting was not implemented for the composite link case, as was done in Buriol, Resende, and Thorup (2006).
- We have recently added a traffic splitting option to our tool.

- We have extended our survivable IP network design tool to handle composite links.
- Min cost heuristic runs fast and finds best-quality solutions.
- In this talk, traffic splitting was not implemented for the composite link case, as was done in Buriol, Resende, and Thorup (2006).
- We have recently added a traffic splitting option to our tool.

- We have extended our survivable IP network design tool to handle composite links.
- Min cost heuristic runs fast and finds best-quality solutions.
- In this talk, traffic splitting was not implemented for the composite link case, as was done in Buriol, Resende, and Thorup (2006).
- We have recently added a traffic splitting option to our tool.

- We have extended our survivable IP network design tool to handle composite links.
- Min cost heuristic runs fast and finds best-quality solutions.
- In this talk, traffic splitting was not implemented for the composite link case, as was done in Buriol, Resende, and Thorup (2006).
- We have recently added a traffic splitting option to our tool.

## My coauthors



Diogo V. Andrade Rutgers University



Mikkel Thorup AT&T Labs Research



Luciana S. Buriol Federal University of Rio Grande do Sul



# The End

