Some applications of biased random-key genetic algorithms in telecommunications

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Summary

- Specifying a biased random-key genetic algorithm
- Applications in telecommunications
 - Routing in IP networks
 - Design of survivable IP networks with composite links
 - Redundant server location for content distribution
 - Regenerator location
 - Routing & wavelength assignment in optical networks
- Concluding remarks



Reference



M.G.C.R., "Biased random-key genetic algorithms with applications in telecommunications," TOP, vol. 20, pp. 120-153, 2012.

Tech report version:

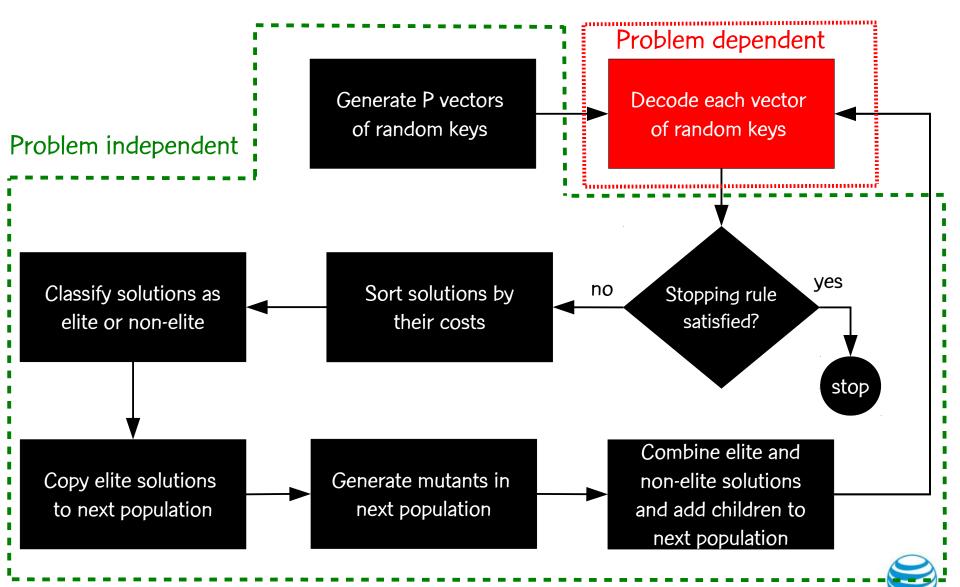
http://www2.research.att.com/~mgcr/doc/brkga-telecom.pdf



Specifying a biased random-key genetic algorithms



Framework for biased random-key genetic algorithms



- Encoding is always done the same way, i.e. with a vector of N random-keys (parameter N must be specified)
- Decoder that takes as input a vector of N random-keys and outputs the corresponding solution of the combinatorial optimization problem and its cost (this is usually a heuristic)

- Size of population
- Size of elite partition
- Size of mutant set
- Child inheritance probability
- Stopping criterion



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- Child inheritance probability: > 0.5, say 0.7
- Stopping criterion: e.g. time, # generations, solution quality,# generations without improvement



Applications in telecommunications



Applications in telecommunications

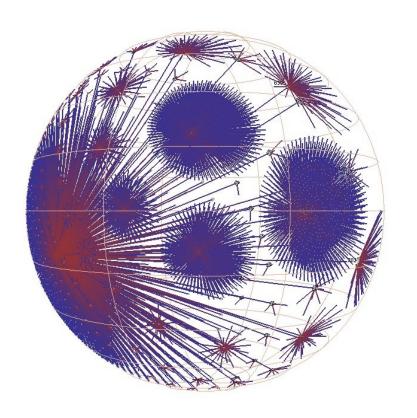
- Routing in IP networks
- Design of survivable IP networks
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- Routing and wavelength assignment in optical networks



OSPF routing in IP networks



The Internet



- The Internet is composed of many (inter-connected) autonomous systems (AS).
- An AS is a network controlled by a single entity, e.g. ISP, university, corporation, country, ...



Global AS-level Map

Routing

- A packet is sent from a origination router S to a destination router T.
- S and T may be in
 - same AS:
 - different ASes:



Routing

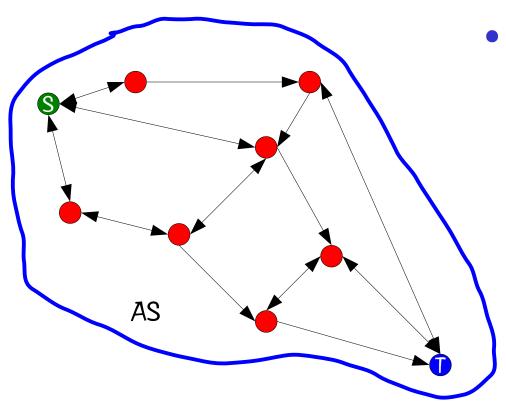
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 - same AS: IGP routing
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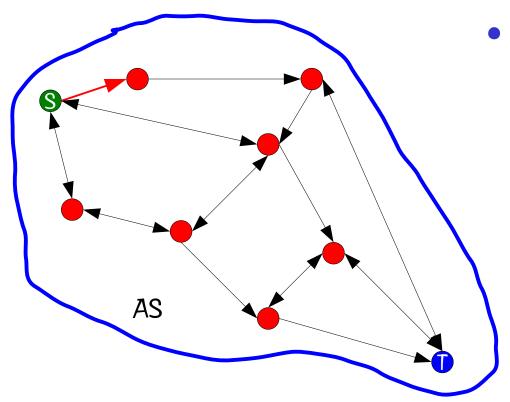
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- A packet is sent from a origination router S to a destination router T.
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 - same AS: IGP routing
 - different ASes: BGP routing

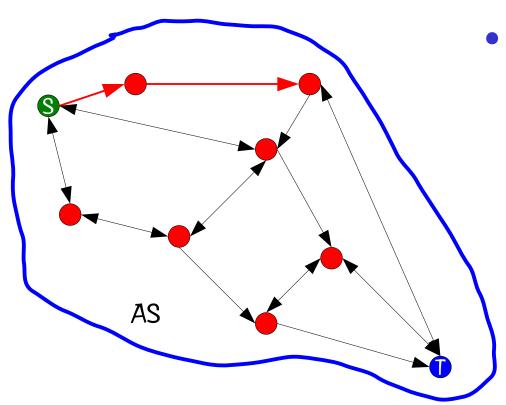




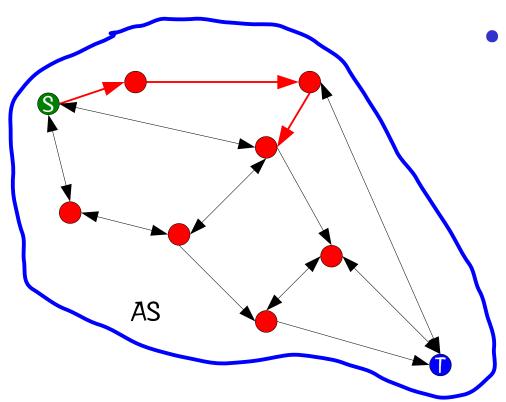




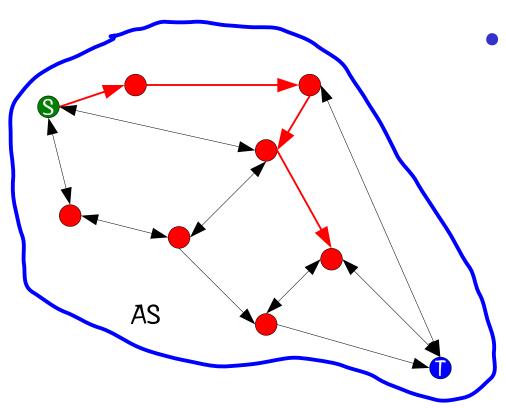




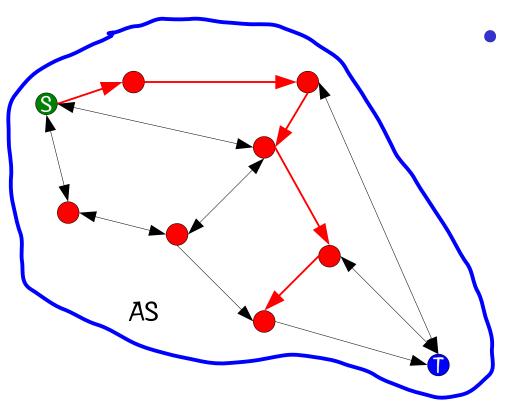




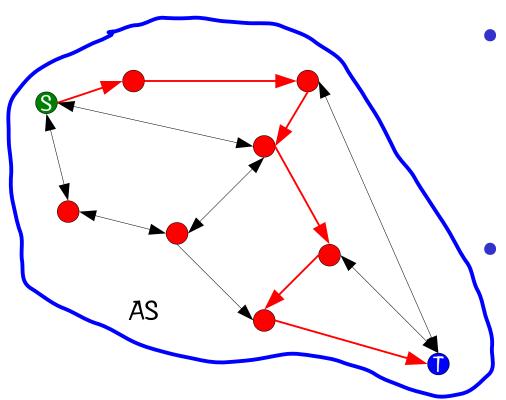






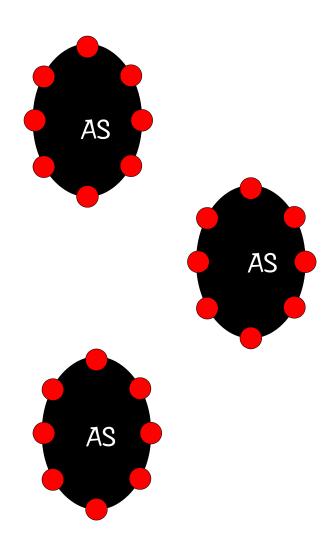




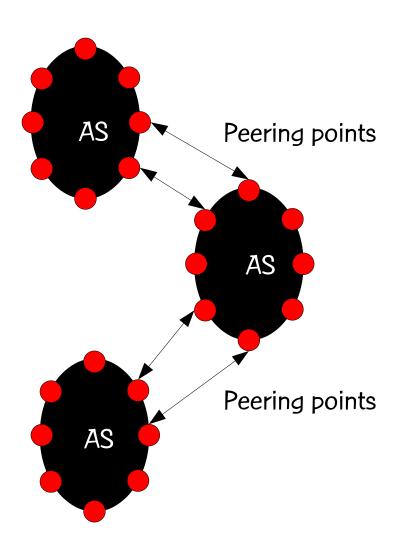


- IGP (interior gateway protocol) routing is concerned with routing within an AS.
- Routing decisions are made by AS operator.

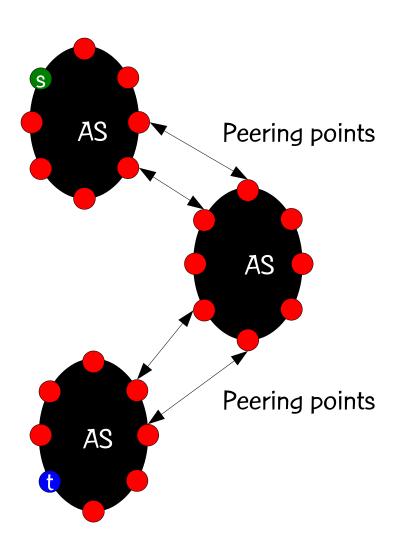




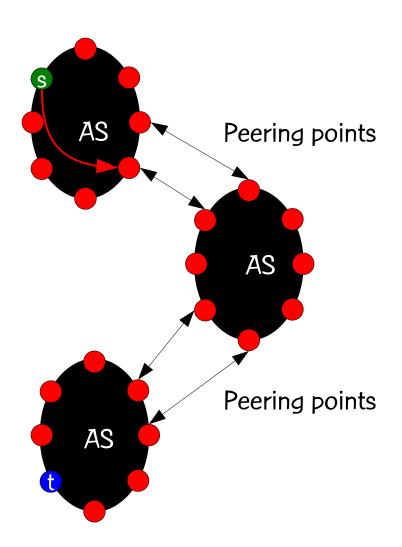




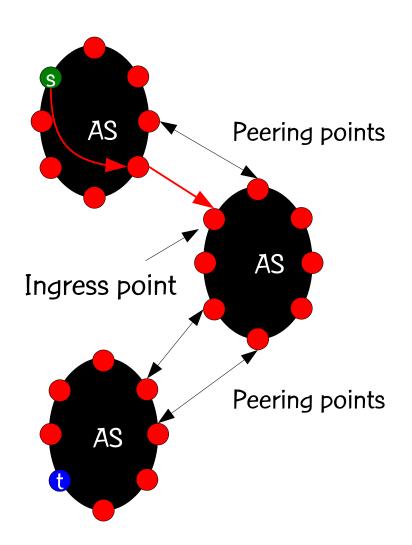




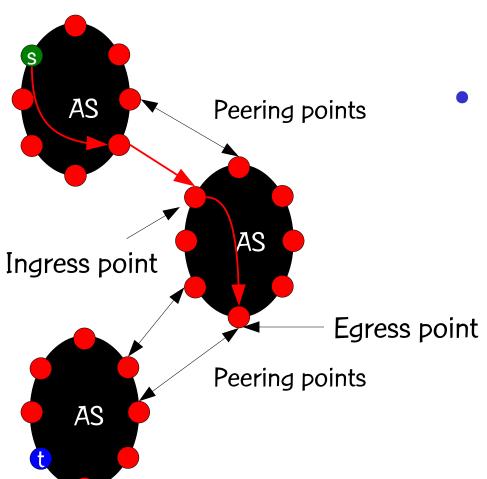




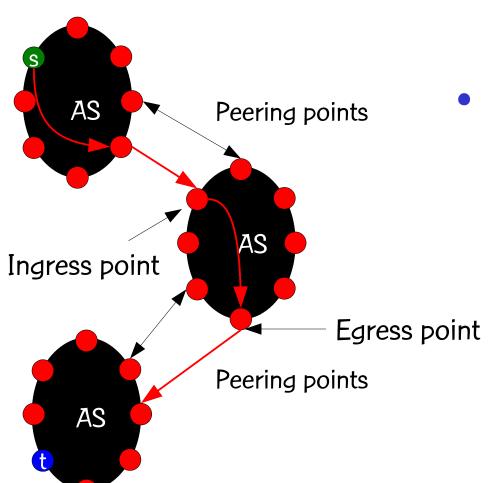




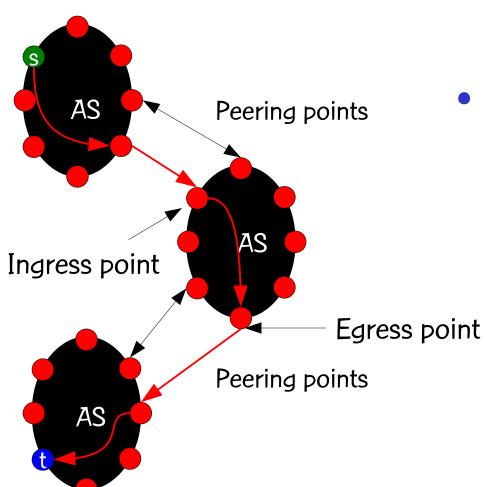
















OSPF routing

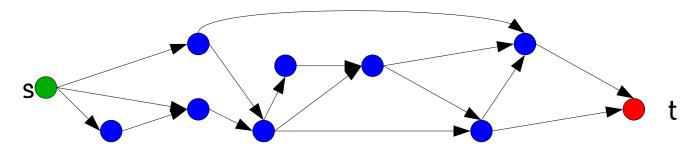
• Given a network G = (N,A), where N is the set of routers and A is the set of links.



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- The OSPF (open shortest path first) routing protocol assumes each link a has a weight w(a) assigned to it so that a packet from a source router s to a destination router t is routed on a shortest weight path from s to t.

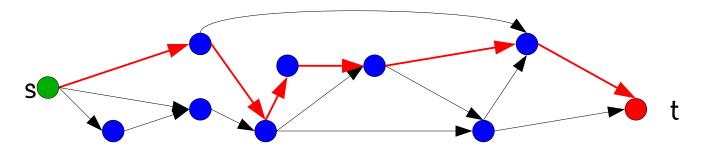


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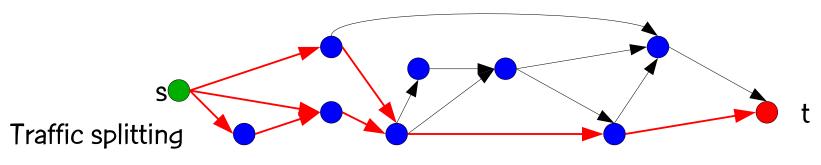


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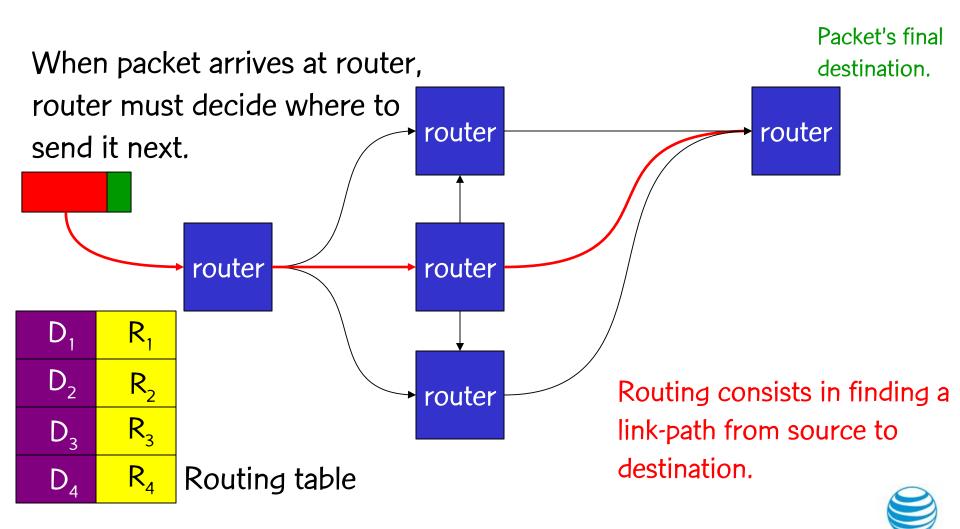
- By setting OSPF weights appropriately, one can do traffic engineering, i.e. route traffic so as to optimize some objective (e.g. minimize congestion, maximize throughput, etc.).
 - Some recent papers on this topic:
 - Fortz & Thorup (2000, 2004)
 - Ramakrishnan & Rodrigues (2001)
 - Sridharan, Guérin, & Diot (2002)
 - Fortz, Rexford, & Thorup (2002)
 - Ericsson, Resende, & Pardalos (2002)
 - Buriol, Resende, Ribeiro, & Thorup (2002, 2005)
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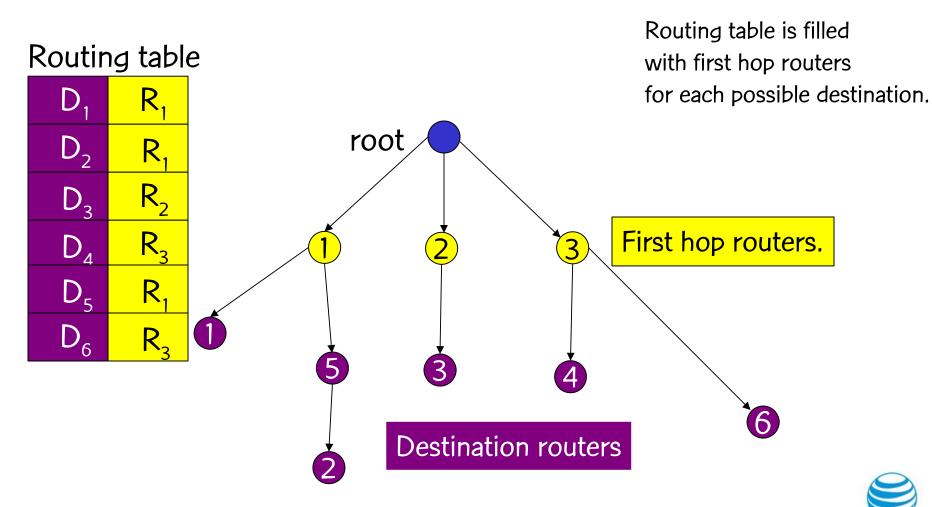


Packet routing

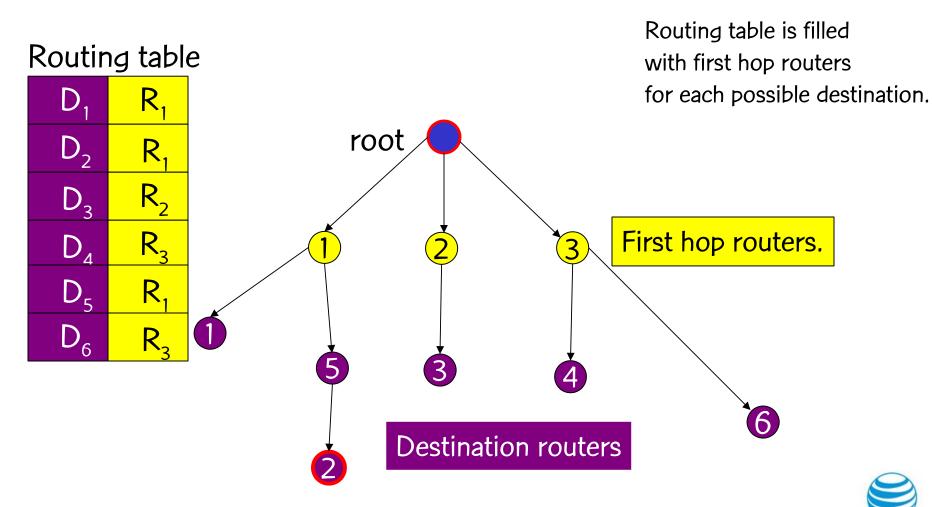


- Assign an integer weight $\in [1, w_{max}]$ to each link in AS. In general, $w_{max} = 65535 = 2^{16} 1$.
- Each router computes tree of shortest weight paths to all other routers in the AS, with itself as the root, using Dijkstra's algorithm.

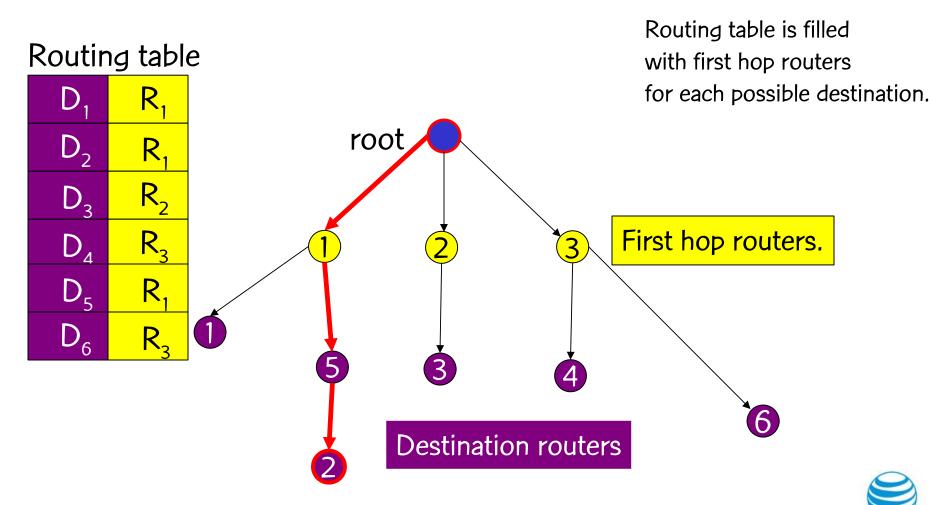




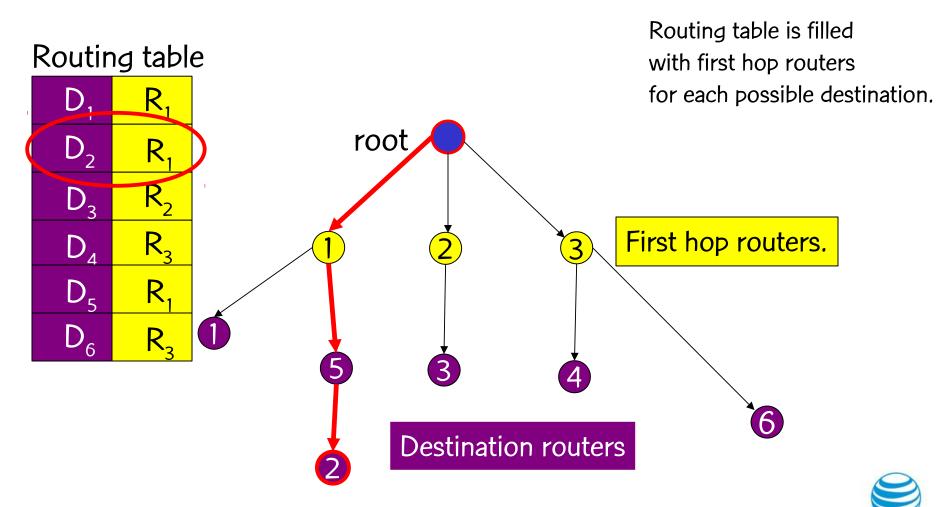




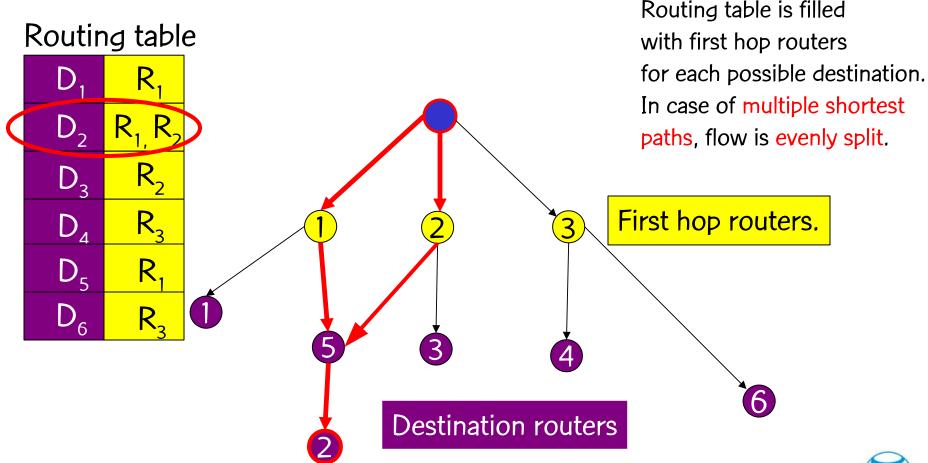












OSPF weight setting

- OSPF weights are assigned by network operator.
 - CISCO assigns, by default, a weight proportional to the inverse of the link bandwidth (Inv Cap).
 - If all weights are unit, the weight of a path is the number of hops in the path.
- We propose two BRKGA to find good OSPF weights.



Minimization of congestion

- Consider the directed capacitated network G = (N,A,c), where N are routers, A are links, and c_a is the capacity of link $a \in A$.
- We use the measure of Fortz & Thorup (2000) to compute congestion:

$$\Phi = \Phi_1(/_1) + \Phi_2(/_2) + \dots + \Phi_{|A|}(/_{|A|})$$

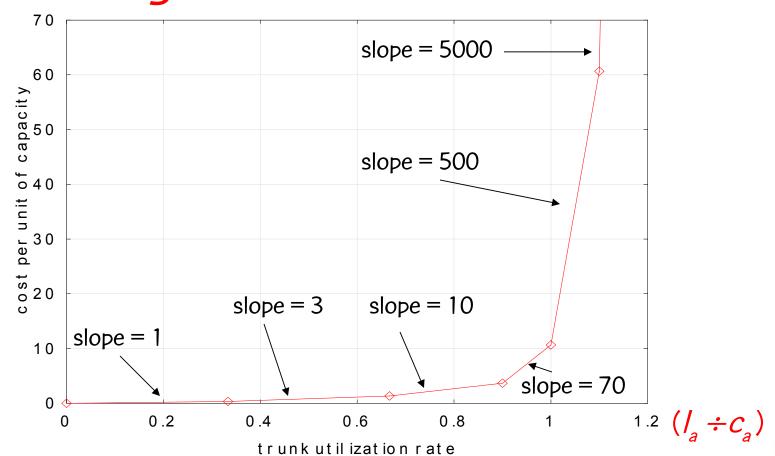
where l_a is the load on link $a \in A$,

 $\Phi_{a}(I_{a})$ is piecewise linear and convex,

$$\Phi_{a}(0) = 0$$
, for all $a \in A$.



Piecewise linear and convex $\Phi_a(I_a)$ link congestion measure





OSPF weight setting problem

- Given a directed network G = (N, A) with link capacities $c_a \in A$ and demand matrix $D = (d_{s,t})$ specifying a demand to be sent from node s to node t:
 - Assign weights $w_a \in [1, w_{max}]$ to each link $a \in A$, such that the objective function Φ is minimized when demand is routed according to the OSPF protocol.





M. Ericsson, M.G.C.R., & P.M. Pardalos, "A genetic algorithm for the weight setting problem in OSPF routing," J. of Combinatorial Optimization, vol. 6, pp. 299–333, 2002.

Tech report version:

http://www2.research.att.com/~mgcr/doc/gaospf.pdf



Ericsson, R., & Pardalos (J. Comb. Opt., 2002)

Encoding:

 A vector X of N random keys, where N is the number of links. The i-th random key corresponds to the i-th link weight.



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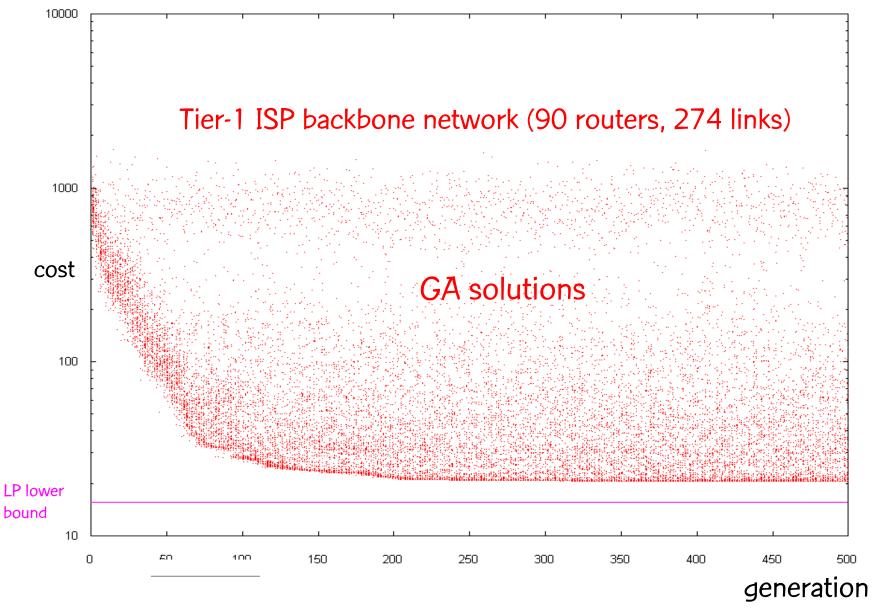
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- Compute shortest paths and route traffic according to OSPF.
- Compute load on each link, compute link congestion, add up all link congestions to compute network congestion.



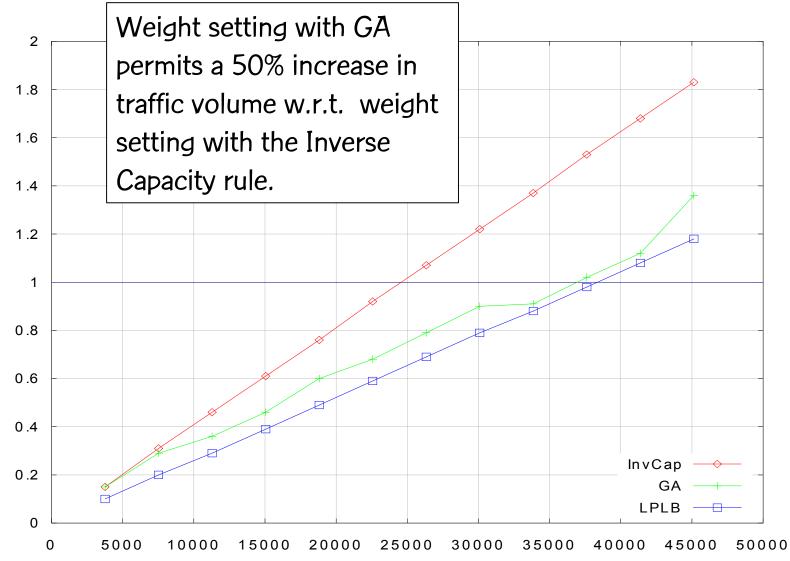


Tier-1 ISP backbone network (90 routers, 274 links)

Weight setting with GA permits a 50% increase in traffic volume w.r.t. weight setting with the Inverse Capacity rule.



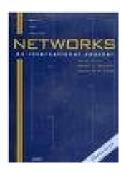
Tier-1 ISP backbone network (90 routers, 274 links)





Max

utilization



L.S. Buriol, M.G.C.R., C.C. Ribeiro, and M. Thorup, "A hybrid genetic algorithm for the weight setting problem in OSPF/IS-IS routing," Networks, vol. 46, pp. 36–56, 2005.

Tech report version:

http://www2.research.att.com/~mgcr/doc/hgaospf.pdf



Buriol, R., Ribeiro, and Thorup (Networks, 2005)

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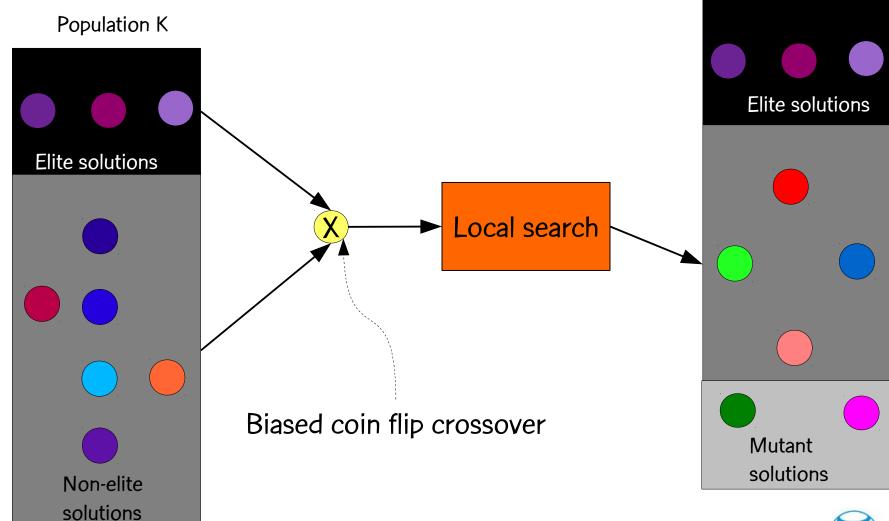
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- Apply fast local search to improve weights.



Decoder has a local search phase

Population K+1



• Let A^* be the set of five arcs $a \in A$ having largest Φ_a values.



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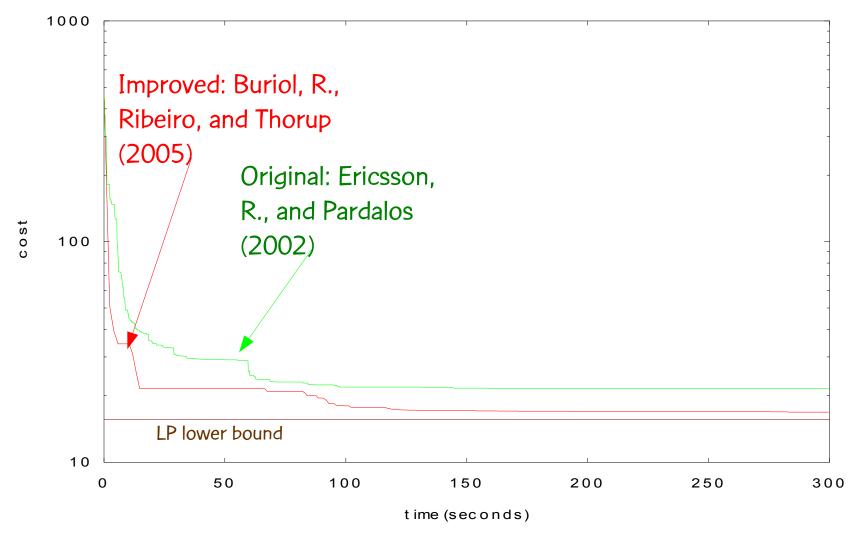
$$[w_a, w_a + [(w_{max} - w_a)/4]]$$



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- Scan arcs $a \in A^*$ from largest to smallest Φ_a :
 - Increase arc weight, one unit at a time, in the range $\begin{bmatrix} w_a, w_a + \lceil (w_{max} w_a)/4 \rceil \end{bmatrix}$
 - If total cost Φ is reduced, restart local search.

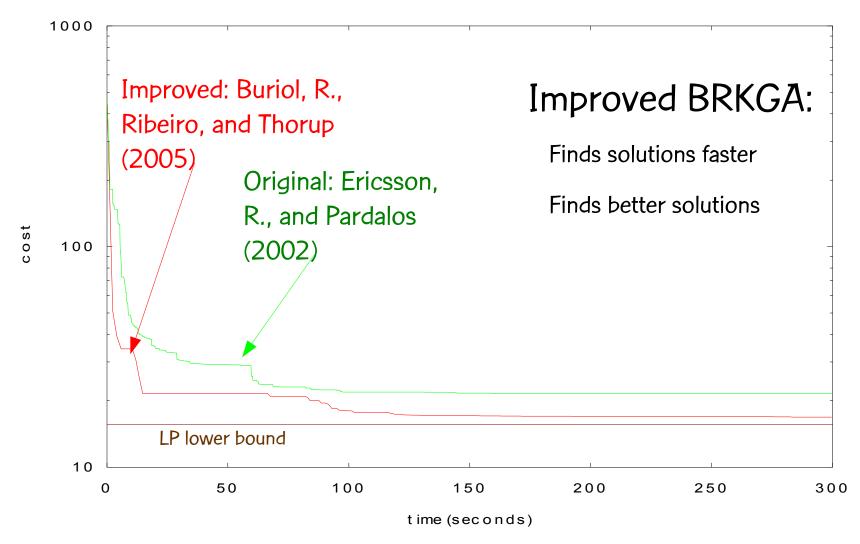


Effect of decoder with fast local search





Effect of decoder with fast local search









L.S. Buriol, M.G.C.R., and M. Thorup, "Survivable IP network design with OSPF routing," Networks, vol. 49, pp. 51–64, 2007.

Tech report version:

http://www2.research.att.com/~mgcr/doc/gamult.pdf



Buriol, R., & Thorup (Networks, 2007)



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Determine

 OSPF weight w(a) to assign to each arc a ∈ A,



Buriol, R., & Thorup (Networks, 2007)

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- OSPF weight w(a) to assign to each arc $a \in A$,
- which arcs should be used to deploy fiber and how many units
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- such that all the demand can be routed on the network even when any single arc fails.
- Min total design cost = $\sum_{a \in A} M(a) \times K(a)$.

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- For each arc a∈ A, determine the multiplicity M(a) using the maximum load for that arc over all failure modes.

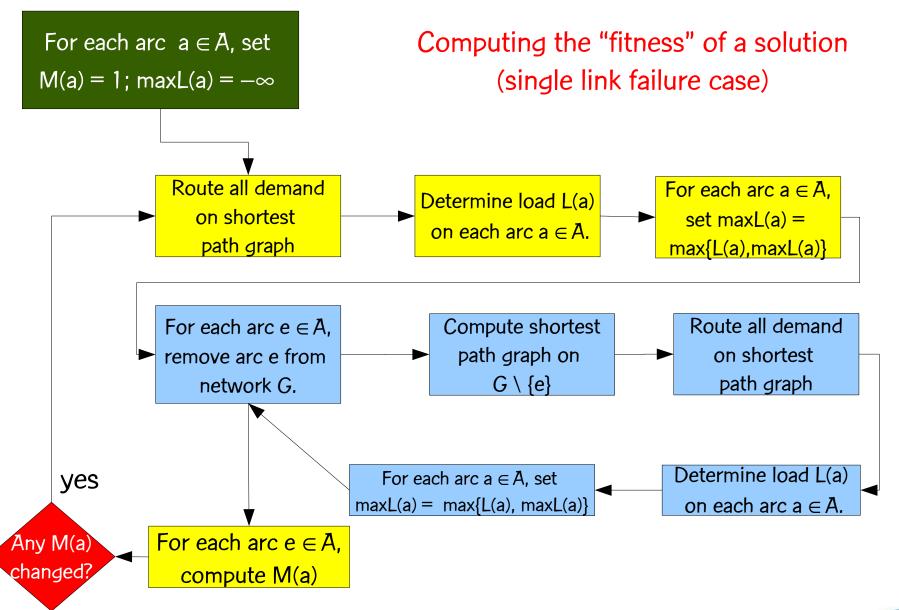


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- For each arc a∈ A, determine the multiplicity M(a) using the maximum load for that arc over all failure modes.
- Network design cost = $\sum_{a \in A} M(a) \times K(a)$









- In Buriol, R., and Thorup (2006)
 - links were all of the same type,
 - only the link multiplicity had to be determined.
- Now consider composite links. Given a load L(a) on arc a, we can compose several different link types that sum up to the needed capacity $c(a) \ge L(a)$:

$$-c(a) = \sum_{t \text{ used in arc a}} M(t) \times \gamma(t)$$
, where

- M(t) is the multiplicity of link type t
- $-\gamma(t)$ is the capacity of link type t



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D.V. Andrade, L.S. Buriol, M.G.C.R., and M. Thorup, "Survivable composite-link IP network design with OSPF routing," The Eighth INFORMS Telecommunications Conference, Dallas, Texas, April 2006.

Tech report:

http://www2.research.att.com/~mgcr/doc/composite.pdf



- Link types = { 1, 2, ..., T }
- Capacities = $\{c(1), c(2), ..., c(T)\}: c(i) < c(i+1)$
- Prices / unit length = { p(1), p(2), ..., p(T) }: p(i) < p(i+1)
 - Assumptions:
 - $[p(T)/c(T)] < [p(T-1)/c(T-1)] < \cdots < [p(1)/c(1)]$, i.e. price per unit of capacity is smaller for links with greater capacity
 - $c(i) = \alpha \times c(i-1)$, for $\alpha \in \mathbb{N}$, $\alpha > 1$, i.e. capacities are multiples of each other by powers of α



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 - $-[p(T)/c(T)] < [p(T-1)/c(T-1)] < \cdots < [p(1)/c(1)]$: economies of scale
 - $-c(i) = \alpha \times c(i-1)$, for $\alpha \in \mathbb{N}$, $\alpha > 1$, e.g. $c(OC192) = 4 \times c(OC48)$; $c(OC48) = 4 \times c(OC12)$; $c(OC12) = 4 \times c(OC3)$;

OC3	OC12	OC48	OC192	
155 Mb/s	622 Mb/s	2.5 Gb/s	10 Gb/s	$\alpha = 4$



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 A vector X of N random keys, where N is the number of links. The i-th random key corresponds to the i-th link weight.



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 type t using the maximum load for that arc over all failure modes.

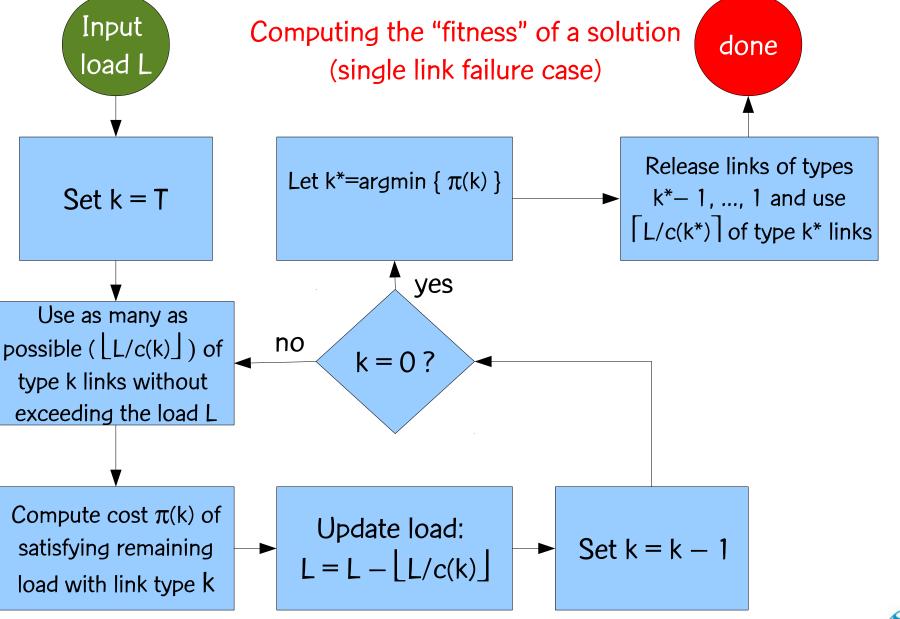


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- Network design cost = $\sum_{i \in A} \sum_{t \text{ used in arc } i} M(t,i) \times p(t)$







Redundant content distribution



Reference:

ALENEX11

Workshop on Algorithm Engineering & Experiments

January 22, 2011 Holiday Inn San Francisco Golden Gateway San Francisco, California USA L. Breslau, I. Diakonikolas, N. Duffield, Y. Gu, M. Hajiaghayi, D.S. Johnson, H. Karloff, M.G.C.R., and S. Sen, "Disjoint-path facility location: Theory and practice," Proceedings of the Thirteenth Workshop on Algorithm Engineering and Experiments (ALENEX11), SIAM, San Francisco, pp. 60–74, January 22, 2011

Tech report version:

http://www2.research.att.com/~mgcr/doc/monitoring-alenex.pdf



Redundant content distribution (RCD)

 Suppose a number of users located at nodes in a network demand content.



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- Copies of content are stored throughout the network in data warehouses.

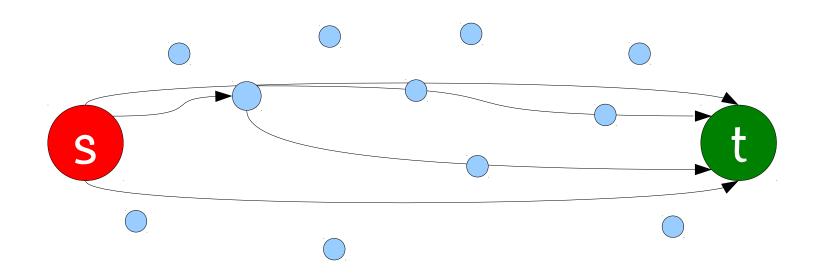


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- Content is sent from data warehouse to user on routes determined by OSPF.



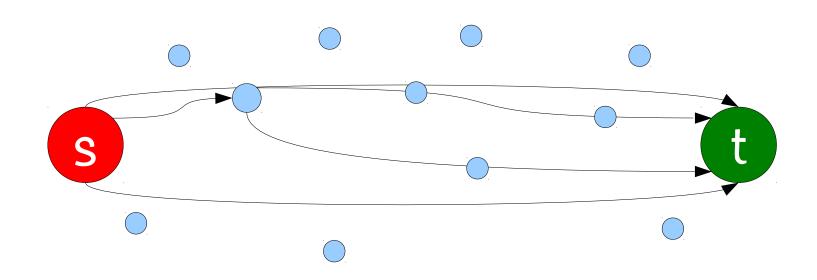
- Suppose a number of users located at nodes in a network demand content.
- Copies of content are stored throughout the network in data warehouses.
- Content is sent from data warehouse to user on routes determined by OSPF.
- Problem: Locate minimum number of warehouses in network such all users get their content even in presence of edge failures.





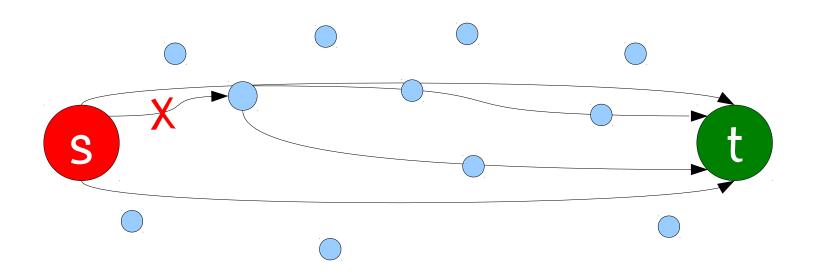
Traffic from node s to node t flows on paths defined by OSPF.





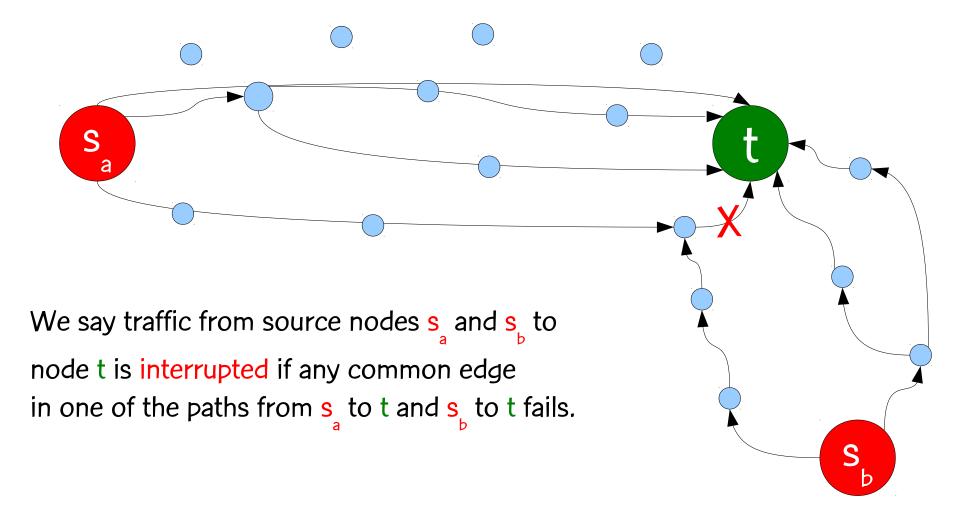
We don't know on which path a particular packet will flow.



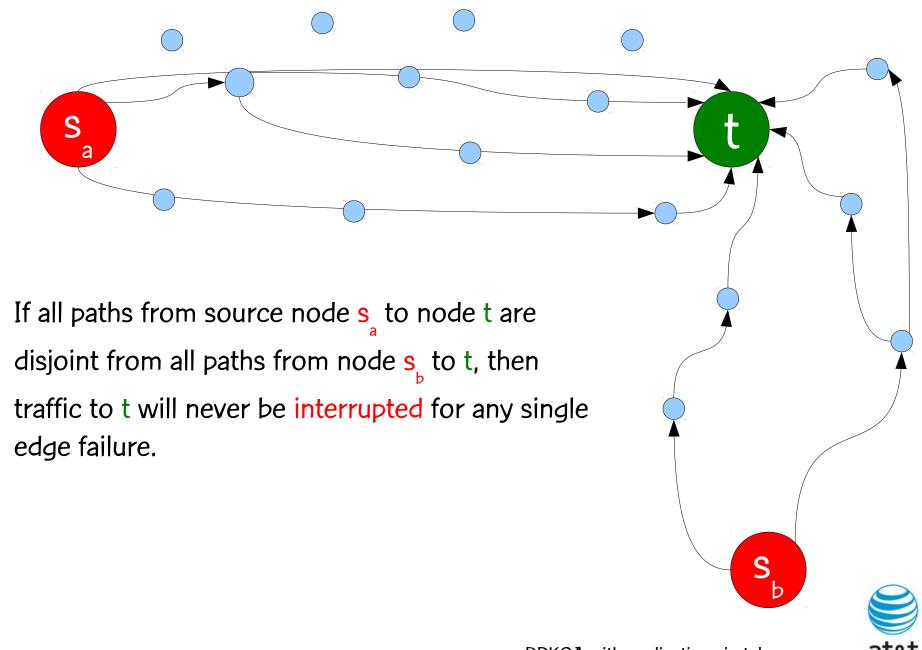


We say traffic from node s to node t is interrupted if any edge in one of the paths from s to t fails.









Suppose nodes b_1 , b_2 , ... want some content (e.g. video).

We want the smallest set **S** of servers such that:

for every b_i there exist m_1 , $m_2 \in \mathbf{S}$ both of which can provide content to b_i

 b_2 b_3 m_4



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 b_2 b_3 m_4



• Given:

- A directed network G = (V, E);
- A set of nodes $B \subseteq E$ where content-demanding users are located;
- A set of nodes M ⊆ E where content warehouses can be located;
- The set of all OSPF paths from m to b, for m ∈ M and $b \in B$.



Compute:

- The set of triples $\{m_1, m_2, b\}^i$, i = 1, 2, ..., T, such that all paths from m_1 to b and from m_2 to b are disjoint, where $m_1, m_2 \in M$ and $b \in B$.
- Note that if $B \cap M \neq \emptyset$, then some triples will be of the type $\{b, b, b, b\}$, where $b \in B \cap M$, i.e. a data warehouse that is co-located with a user can provide content to the user by itself.



- Solve the covering by pairs problem:
 - Find a smallest-cardinality set M*⊆ M such that for all b∈ B, there exists a triple { m₁, m₂, b } in the set of triples such that m₁, m₂∈ M*.



initialize partial cover M* = { }



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- while M* is not a cover do:



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 - if no m ∈ M \ M* yields an increase in coverage, then choose a pair $\{m_1, m_2\}$ ∈ M \ M* that yields a maximum increase in coverage and set M* = M* \cup $\{m_1\}$ \cup $\{m_2\}$



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- while M* is not a cover do:
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 - if no $m \in M \setminus M^*$ yields an increase in coverage, then choose a pair $\{m_1, m_2\} \in M \setminus M^*$ that yields a maximum increase in coverage and set $M^* = M^* \cup \{m_1\} \cup \{m_2\}$
 - if no pair exists, then the problem is infeasible



BRKGA for redundant content distribution



Encoding:

— A vector X of N keys randomly generated in the real interval (0,1], where N = |M| is the number of potential data warehouse nodes. The i-th random key corresponds to the i-th potential data warehouse node.



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Decoder:

- For i = 1, ..., N: if $X(i) > \frac{1}{2}$, add i-th data warehouse node to solution



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Decoder:

- For i = 1, ..., N: if $X(i) > \frac{1}{2}$, add i-th data warehouse node to solution
- If solution is feasible, i.e. all users are covered: STOP
- Else, apply greedy algorithm to cover uncovered user nodes.



- Size of population: N (number of monitoring nodes)
- Size of elite set: 15% of N
- Size of mutant set: 10% of N
- Biased coin probability: 70%
- Stop after N generations without improvement of best found solution



 Internet service provider (ISP) delivers virtual private network (VPN) service to customers.



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- The ISP agrees to send traffic between locations specified by the customer and promises to provide certain level of service on the connections.

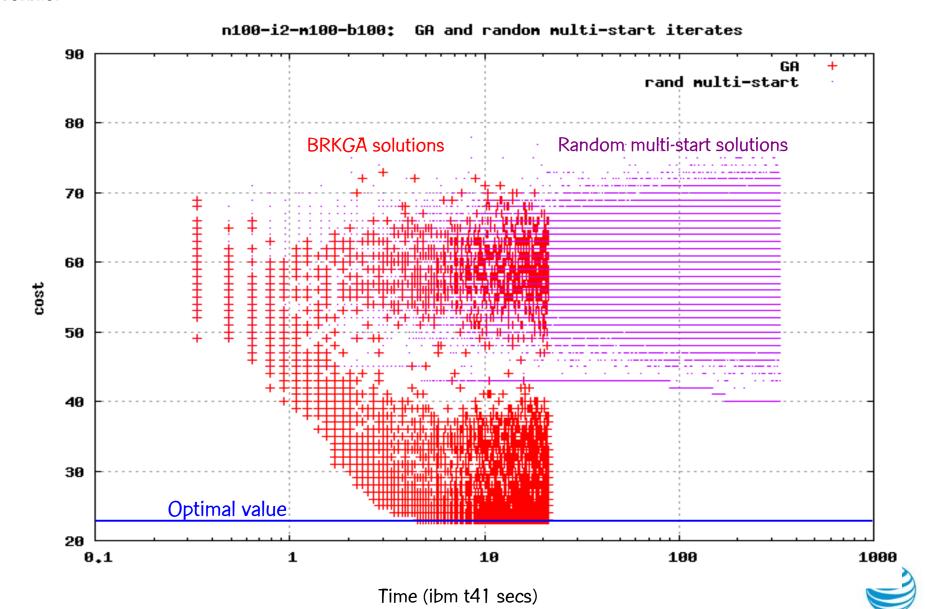


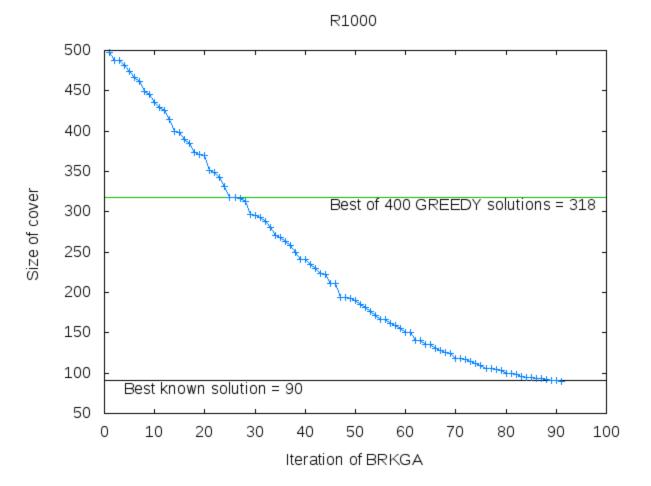
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- The ISP agrees to send traffic between locations specified by the customer and promises to provide certain level of service on the connections.
- A key service quality metric is packet loss rate.
- We want to minimize the number of monitoring equipment placed in the network to measure packet loss rate: This is a type of covering by pairs problem.

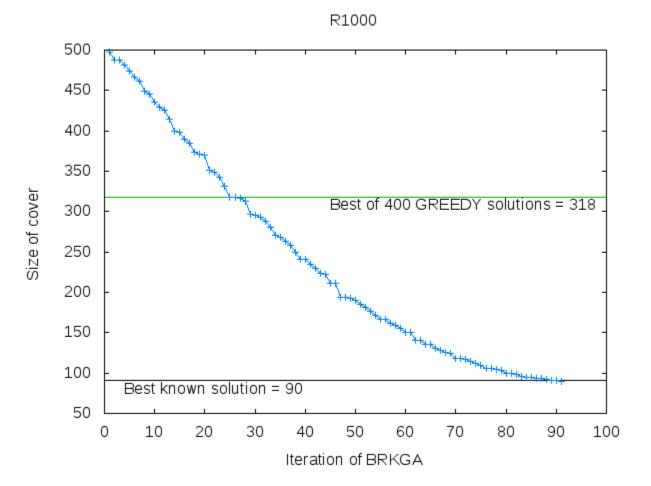






Real-world instance derived from a proprietary Tier-1 Internet Service Provider (ISP) backbone network using OSPF for routing.





Size of network: about 1000 nodes, where almost all can store content and about 90% have content-demanding users. Over 45 million triples.



Regenerator location problem



Reference

A. Duarte, R. Martí, M.G.C.R., and R.M.A. Silva, "Improved heuristics for the regenerator location problem," International Transactions in Operational Research, to appear in 2014.

Tech report version:

http://www.research.att.com/~mgcr/doc/gpr-regenloc.pdf



 Telecommunication systems use optical signals to transmit information



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- Strength of signal deteriorates and loses power as it gets farther from source



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- Strength of signal deteriorates and loses power as it gets farther from source
- Signal must be regenerated periodically to reach destination: Regenerators
- Regenerators are expensive: minimize the number of regenerators in the network



Given:

- Graph G=(V,E), where V are vertices, E are edges, where edge (i,j) has a real-valued length d(i,j) > 0
- D is the maximum length that a signal can travel before it must regenerated



- Find:
 - Paths that connect all pairs of nodes in V×V
 - Nodes where it is necessary to locate single regenerators
- Minimize number of deployed regenerators



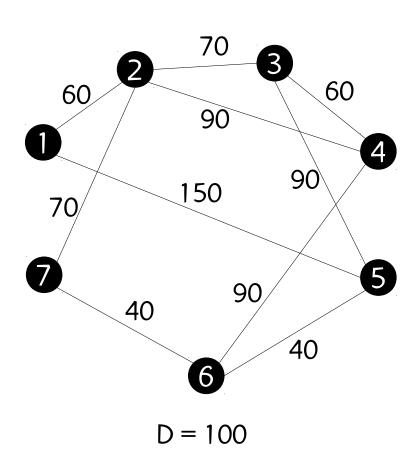
- Path between {s,t} ∈ E
 - { (s,v[1]), (v[1],v[2]), ...,(v[k],t) } is formed by one or more path segments
- Path segment is sequence of consecutive edges
 - { (v[i],v[i+1]), (v[i+1],v[i+2]), ...,(v[q-1],v[q]) } in the path satisfying the condition

 $d(v[i],v[i+1]) + d(v[i+1],v[i+2]) + \cdots + (v[q-1],v[q]) \le D$



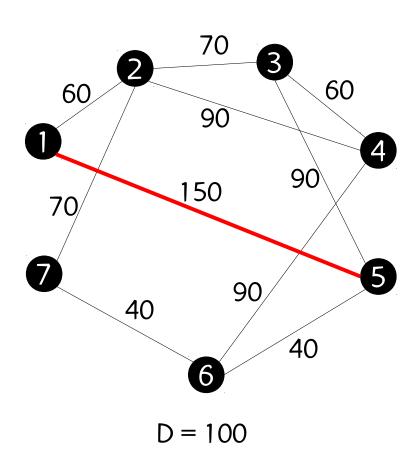
- If total length of path is no more than D, then path consists of a single path segment
- Otherwise, it consists of one or more segments
 - Regenerators will be located in the internal nodes of the path





7-node graph with D = 100

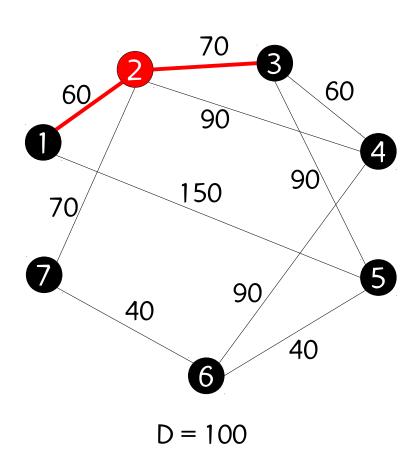




(1) Note that:

- -D(1,5) = 150 > 100 = D
- Edge (1,5) cannot be part of any path



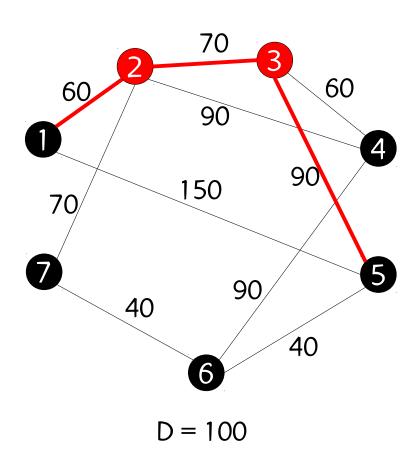


(2) Note that:

Shortest path from 1 to 3 is
 { (1,2), (2,3) } with total
 length
 60 + 70 = 130 > 100 = D

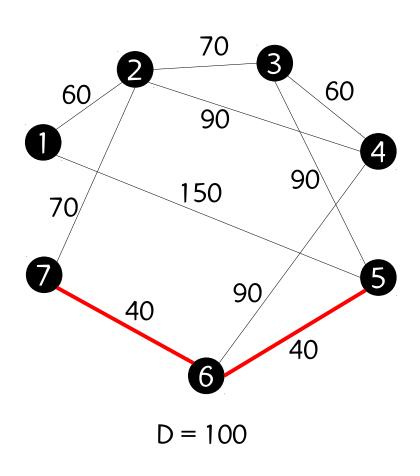
Must be decomposed into two path segments { (1,2) } and { (2,3) } with a regenerator in node 2





(3) Note that:

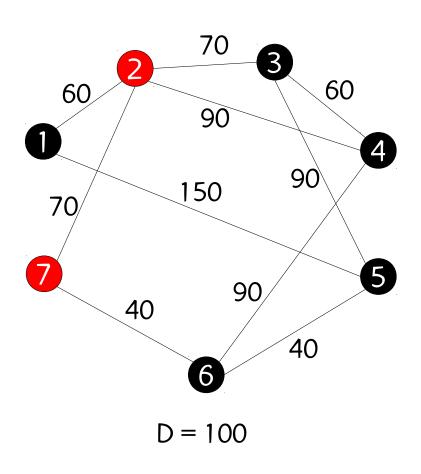
- Shortest feasible path from 1 to 5 is { (1,2), (2,3), (3,5) } with total length
 60 + 70 + 90 = 220 >
 100 = D
- Must be decomposed into three path segments { (1,2) },
 { (2,3) }, and { (3,5) } with regenerators in nodes 2 and 3



(4) Note that:

- Shortest feasible path from 5 to 7 is $\{(5,6), (6,7)\}$ with total length $40 + 40 = 80 \le$ 100 = D
- No regenerator is needed to connect nodes 5 and 7

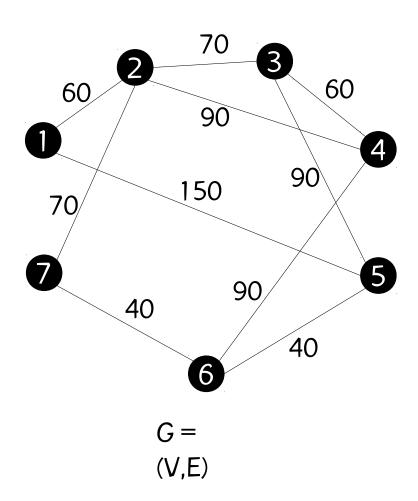




(5) Note that:

 Placing regenerator in nodes 2 and 7 allows for communication between all pairs of nodes in the graph

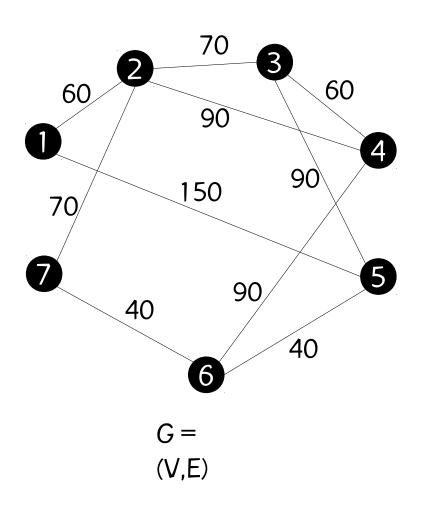


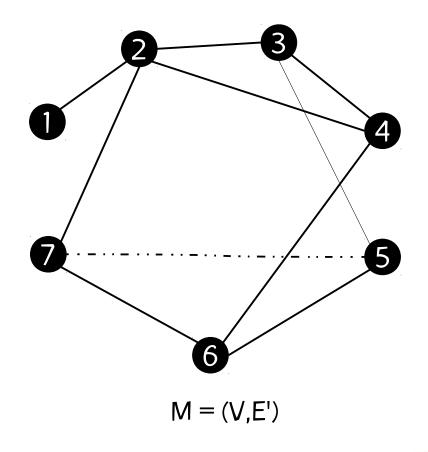


Given weighted graph G

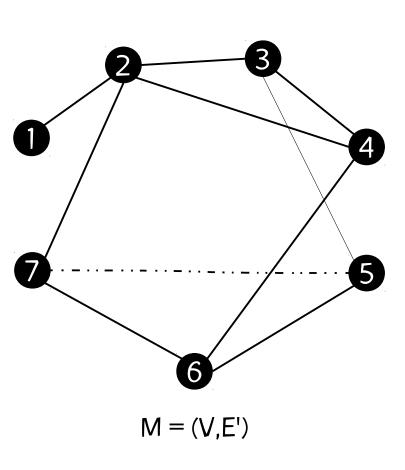
- Delete all edges having length greater than D
- For all non-adjacent nodes,
 add an edge between them
 of length equal to the
 corresponding shortest path
 in G if it is less than D
- Disregard all length info





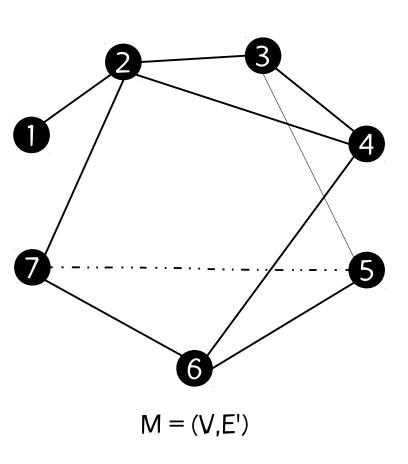






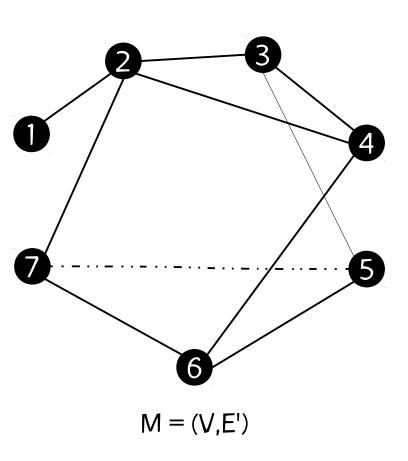
 If M is complete, then there is no need for regenerators





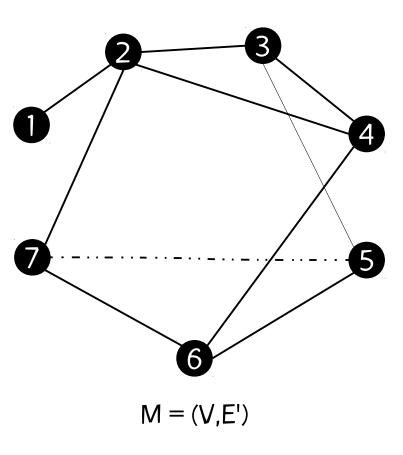
- If M is complete, then there is no need for regenerators
- If M is not connected, then the problem is infeasible





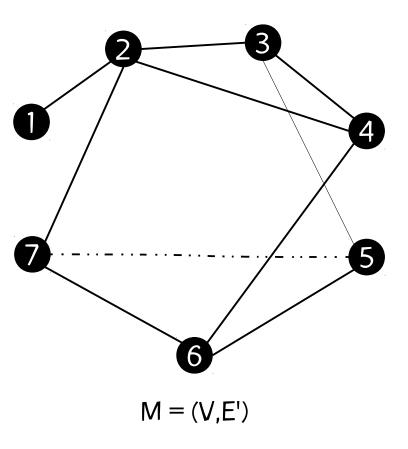
- If M is complete, then there is no need for regenerators
- If M is not connected, then the problem is infeasible
- Otherwise, one or more regenerators are needed





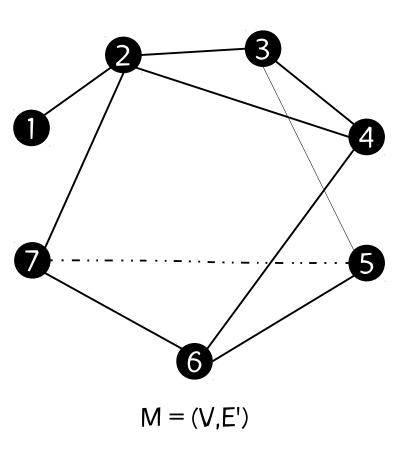
Works on communication graph M





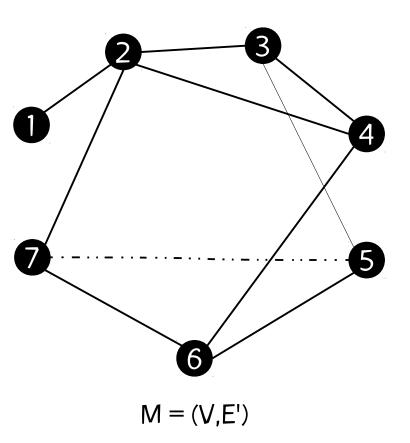
- Works on communication graph M
- Input: set of nodes not directly connected (NDC) in M and builds a set R of regenerator nodes





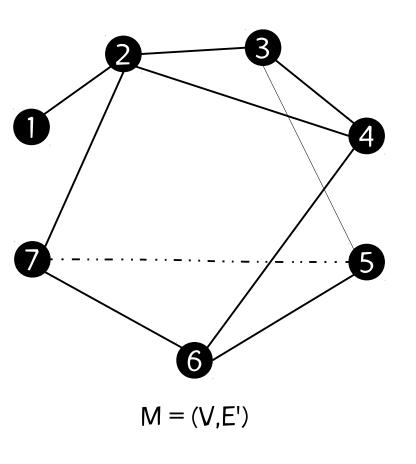
- Works on communication graph M
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- At each step the procedure determines a node u* whose inclusion in R enables the connection of the largest number g(u*) of yet unconnected pairs X(u*) in M



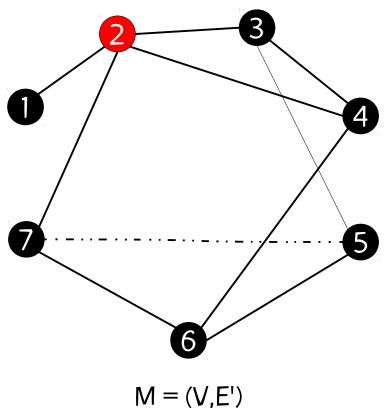


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- Input: set of nodes not directly connected (NDC) in M and builds a set R of regenerator nodes
- At each step the procedure determines a node u* whose inclusion in R enables the connection of the largest number g(u*) of yet unconnected pairs X(u*) in M
- Node u* is added to R and M is updated



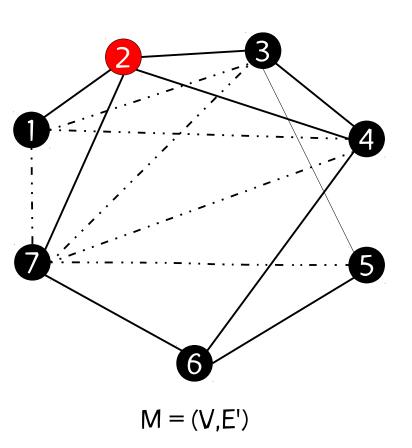


U	X(u)	g(u)
1	Ø	0
2	$\{(1,3),(1,4),(1,7),(3,7),(4,7)\}$	5
3	{ (4,5),(2,5) }	2
4	{ (2,6),(3,6) }	2
5	{ (3,7),(3,6) }	2
6	{ (4,7),(4,5) }	2
7	{ (2,6),(2,5) }	2
		2404



Add regenerator to node 2

U	X(u)	g(u)
1	Ø	0
2	{ (1,3),(1,4),(1,7),(3,7), (4.7) }	5
3	{ (4,5),(2,5) }	2
4	{ (2,6),(3,6) }	2
5	{ (3,7),(3,6) }	2
6	{ (4,7),(4,5) }	2
7	{ (2,6),(2,5) }	2
	BRKGA with applications in telecom	at&t



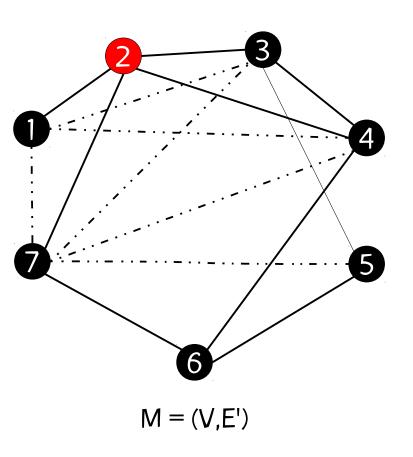
	U	X(u)	g(u)
	1	Ø	0
	2	{ (1,3),(1,4),(1,7),(3,7), (4.7) }	5
	3	{ (4,5),(2,5) }	2
	4	{ (2,6),(3,6) }	2
	5	{ (3,7),(3,6) }	2
	6	{ (4,7),(4,5) }	2
or	7	{ (2.6).(2.5) }	2

Update M to account for regenerator

in node 2

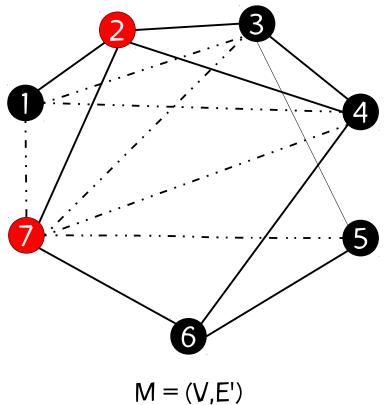
BRKGA with applications in telecom

Summer School in O.R. & Appl. - May 14, 2014



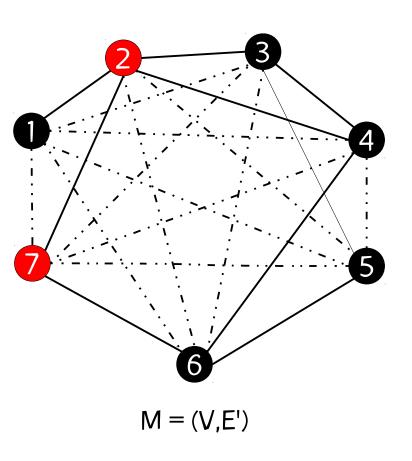
u	X(u)	g(u)
1	Ø	0
-	-	-
3	{ (1,5),(2,5),(4,5) }	3
4	{ (1,6),(2,6),(3,6) }	3
5	{ (3,6) }	1
6	{ (4,5) }	1
7	{ (1,5),(1,6),(2,5),(2,6),(3,6),(4,5) }	6





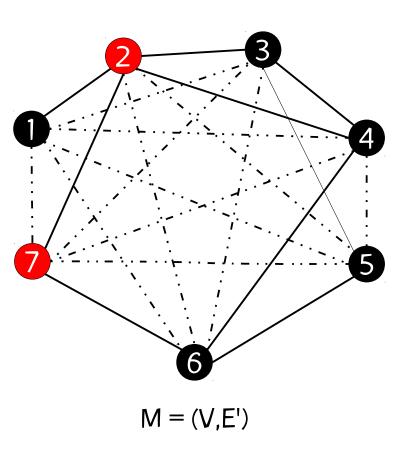
Add regenerator to node 7

u	X(u)	g(u)
1	Ø	0
-	-	-
3	{ (1,5),(2,5),(4,5) }	3
4	{ (1,6),(2,6),(3,6) }	3
5	{ (3,6) }	1
6	{ (4,5) }	1
7	{ (1,5),(1,6),(2,5),(2,6),(3,6),(4,5) }	6



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Since M is complete, all pairs can communicate and solution $R = \{2,7\}$



BRKGA for the regenerator location problem



Encoding

Solutions are encoded as vectors Y of n = |V| random keys, each in the real interval [0,1)

Random key Y[i] corresponds to node $i \in V$



Decoding

Takes as input a communication graph M = (V,E') and a vector of random keys Y

Outputs a set of regenerator nodes $R \subseteq V$



Decoding

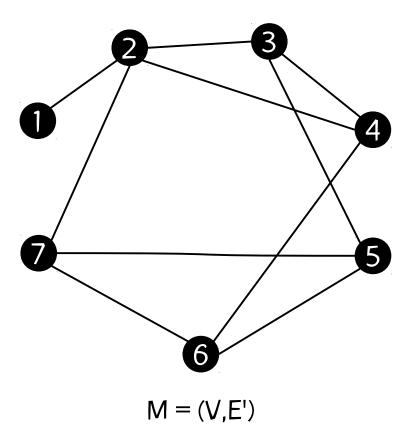
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Outputs a set of regenerator nodes $R \subseteq V$

Sorting Y implies an ordering of V



Decoding



Scan V in order implied by Y

while come pair in $V \times V$ cannot communicate (M = (V, E') is not complete):

Add next vertex v in order into R

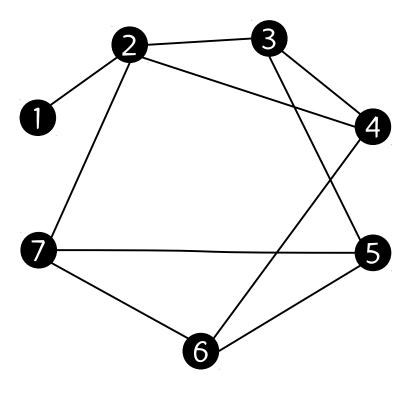
Compute set X of pairs that do not communicate that would if v becomes a regenerator

Add X to E'

end while

return R





X = (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7)

Scan V in order implied by Y

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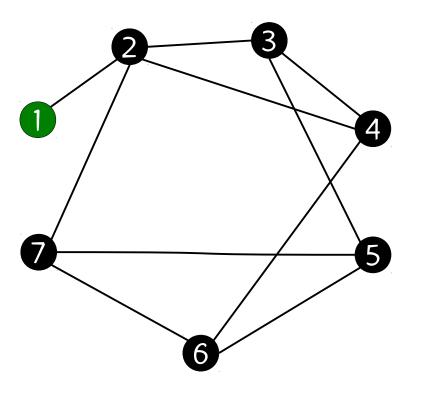
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$$i = 1$$

Scan V in order implied by Y

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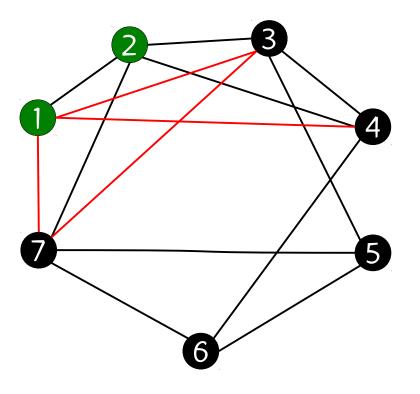
Add next vertex v in order into R

Compute set X of pairs that do not communicate that would if v becomes a regenerator

Add X to E'

end while





$$X = (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7)$$

$$i = 2$$

Scan V in order implied by Y

while come pair in $V \times V$ cannot communicate (M = (V, E') is not complete):

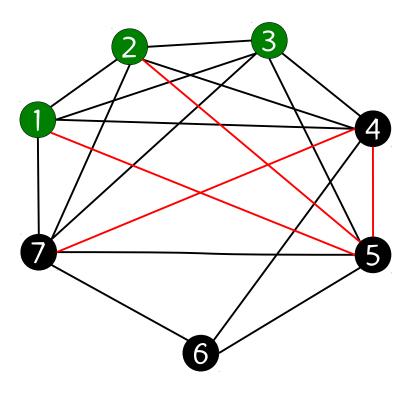
Add next vertex v in order into R

Compute set X of pairs that do not communicate that would if v becomes a regenerator

Add X to E'

end while





$$X = (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7)$$

$$1 = 3$$

Scan V in order implied by Y

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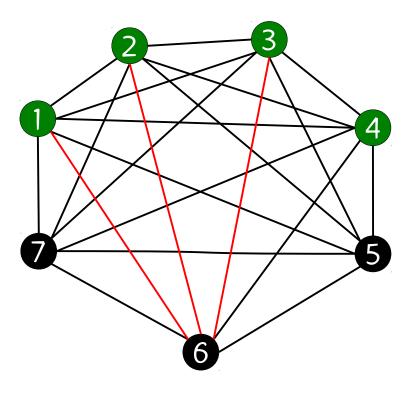
Add next vertex v in order into R

Compute set X of pairs that do not communicate that would if v becomes a regenerator

Add X to E'

end while





$$X = (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7)$$

$$i = 4$$

Scan V in order implied by Y

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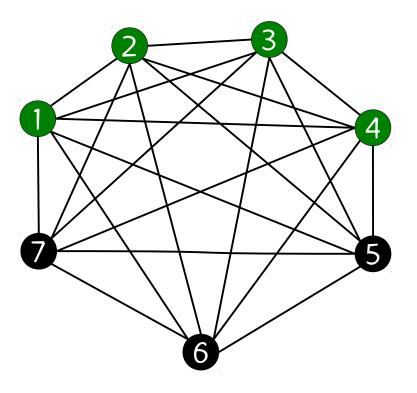
Add next vertex v in order into R

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Add X to E'

end while





M is complete!

$$R = \{ 1, 2, 3, 4 \}$$

Scan V in order implied by Y

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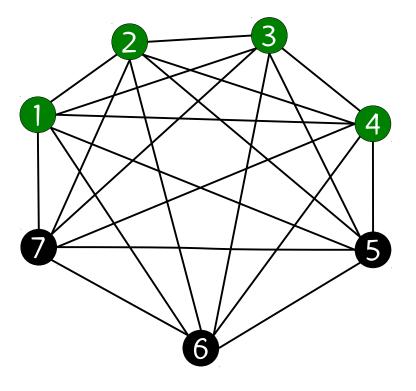
Add next vertex v in order into R

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end while





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Compute set X of pairs that do not communicate that would if v becomes a regenerator

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end while local search return R



Routing and wavelength assignment in optical networks



 Objective: Route a set of connections (called lightpaths) and assign a wavelength to each of them.



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- Connections whose paths share a common link in the network are assigned to different wavelengths (wavelength clash constraint).
- If no wavelength converters are available, the same wavelength must be assigned along the entire route (wavelength continuity constraint).



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 - Asymmetric traffic matrices and bidirectional links.
 - NP-hard (Erlebach and Jansen, 2001)



Connections

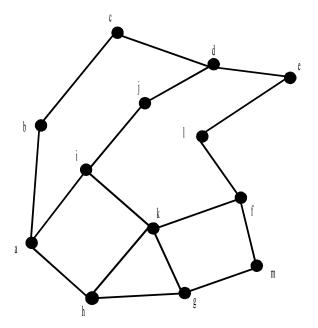
 $c \leftrightarrow m$

 $d \leftrightarrow b$

 $e \leftrightarrow h$

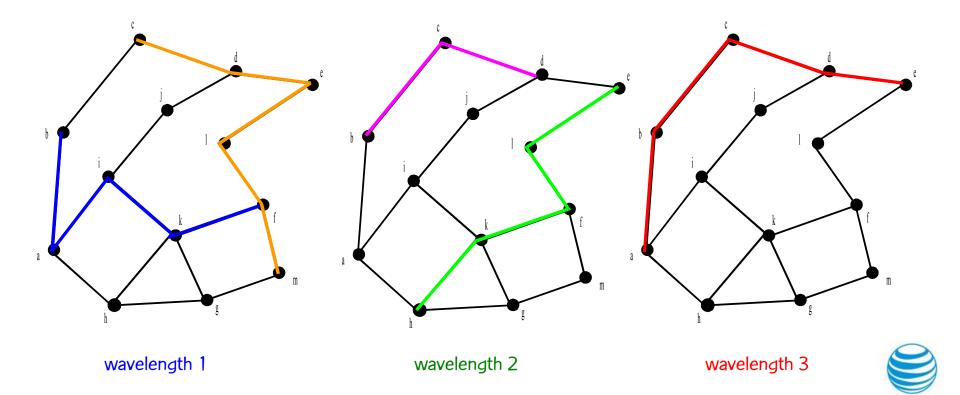
 $a \leftrightarrow e$

 $b \leftrightarrow f$





Connections: $(a \leftrightarrow e) (b \leftrightarrow f) (c \leftrightarrow m) (d \leftrightarrow b) (e \leftrightarrow h)$



Heuristic of N. Skorin-Kapov (EJOR, 2007)

- Associates the min-RWA with the bin packing problem.
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 - Best Fit Decreasing (BFD): state of the art heuristic for RWA



Efficient implementation of BFD-RWA



T.F. Noronha, M.G.C.R., and C.C. Ribeiro,

"Efficient implementations of heuristics for routing and wavelength assignment," in "Experimental Algorithms,"

7th International Workshop (WEA 2008), C.C. McGeoch (Ed.), LNCS, vol. 5038, pp. 169-180, Springer, 2008.

Tech report version:

http://www.research.att.com/~mgcr/doc/impl_rwa_heur.pdf



BFD-RWA

N. Skorin-Kapov (2007); Noronha, R., and Ribeiro (2008)

- Input:
 - A directed graph G representing the network topology.
 - A set T of connection requests.
 - The value d of of the maximum number of arcs in each route. It is set to be the maximum of the square root of the number of links in the network and the diameter of G.
- Starts with only one copy of G (called G₁).
- Connections are selected according to non-increasing order of the lengths of their shortest paths in G_i. Ties are broken at random.
- The connection is assigned wavelength i, and the arcs along path are deleted from G_i .
- If no existing bin can accommodate the connection with fewer than d arcs, a new bin is created.



T.F. Noronha, M.G.C.R., and C.C. Ribeiro, "A biased random-key genetic algorithm for routing and wavelength assignment," J. of Global Optimization, vol. 50, pp. 503–518, 2011.

Tech report version:

http://www.research.att.com/~mgcr/doc/garwa-full.pdf



Noronha, R., and Ribeiro (2011)

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- Decoding:
 - 1) Sort the connection in set T in non-increasing order of $c(i) = SP(i) \times 10 + X[i]$, for each connection $i \in T$.
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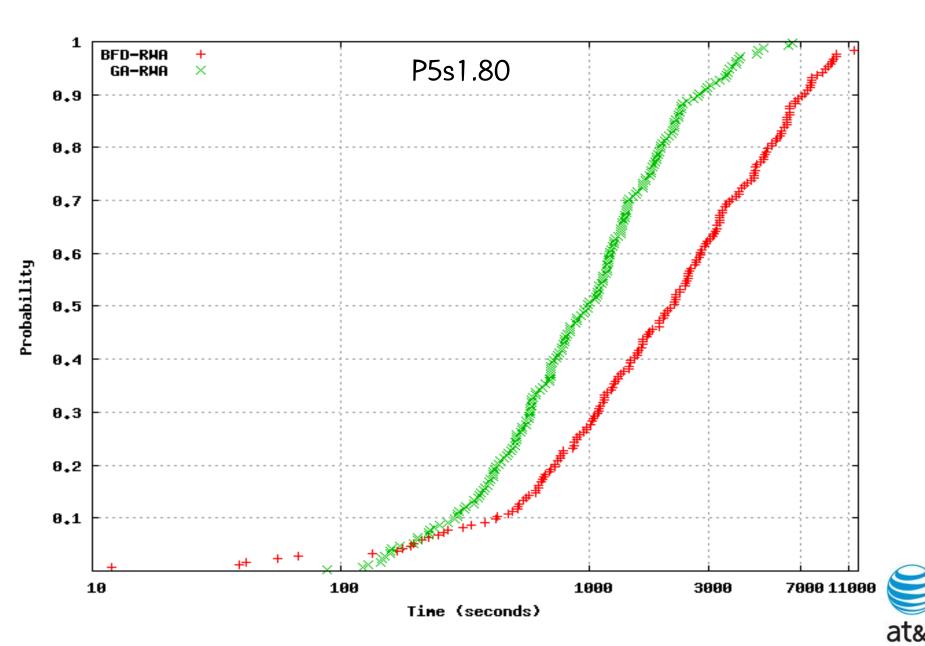
Since there are many ties connection pairs with The same SP(i) value, in the original algorithm of Skorin-Kapov, ties are broken at random. In the BRKGA, the algorithm "learns" how to break ties.

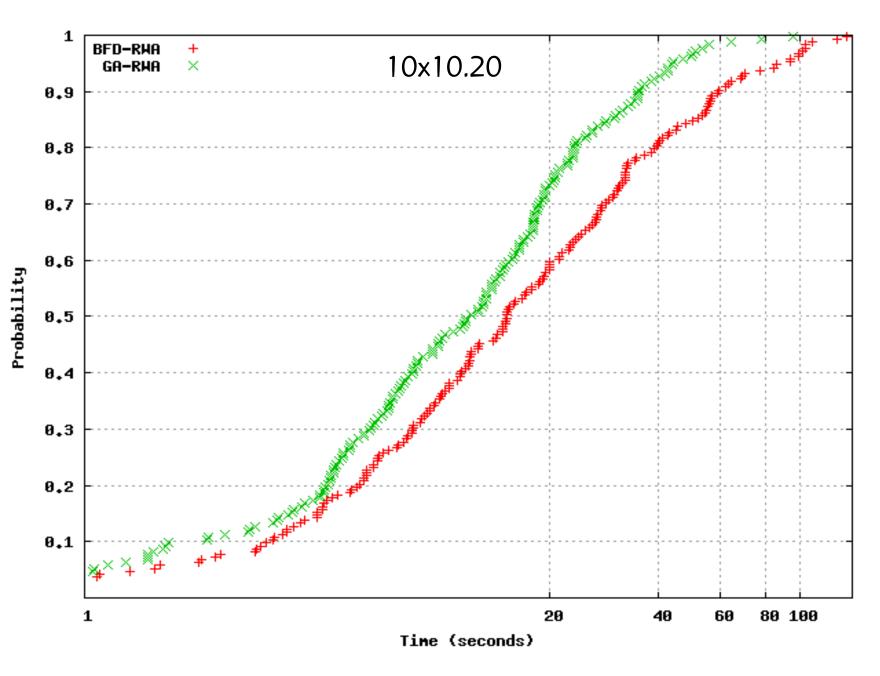


Experiments

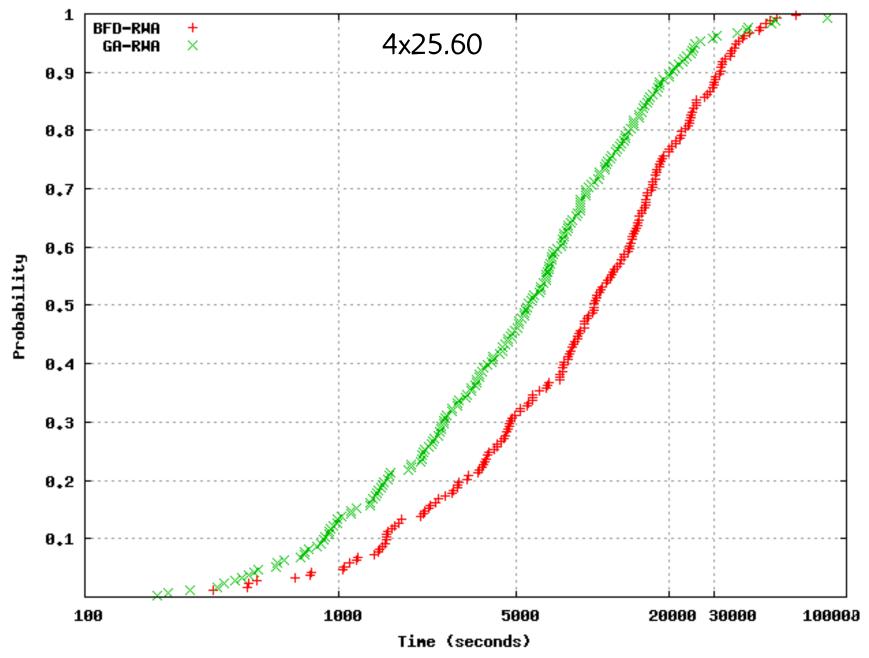
- Compare multi-start version of Skorin-Kapov's heuristic (MS-RWA) with GA-RWA.
- Make 200 independent runs of each heuristic of each heuristic on five instances, stopping when target solution was found (target was set to be best solution found by MS-RWA after 10,000 multi-start iterations.
- Plot CDF (runtime distribution) for each heuristic.



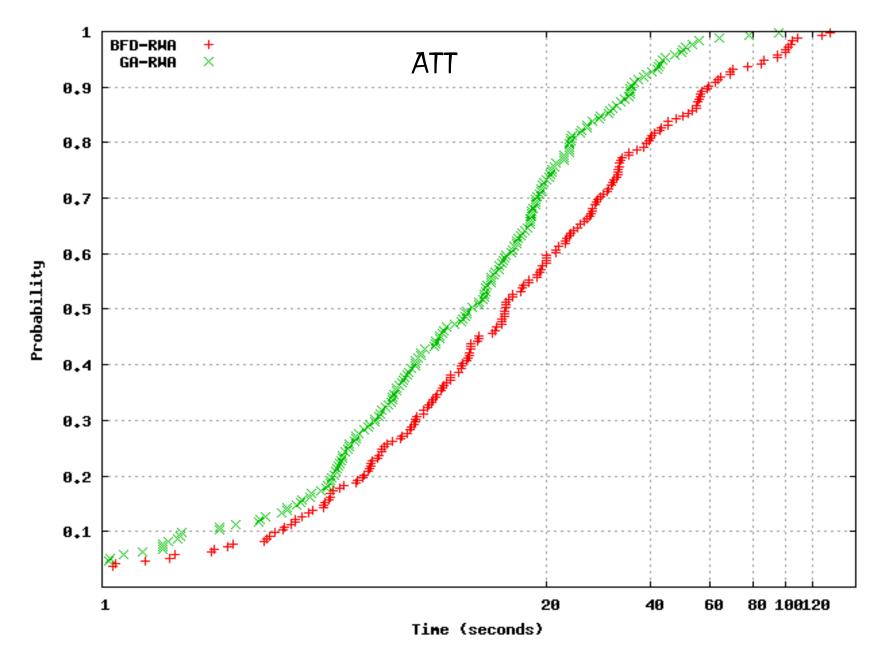




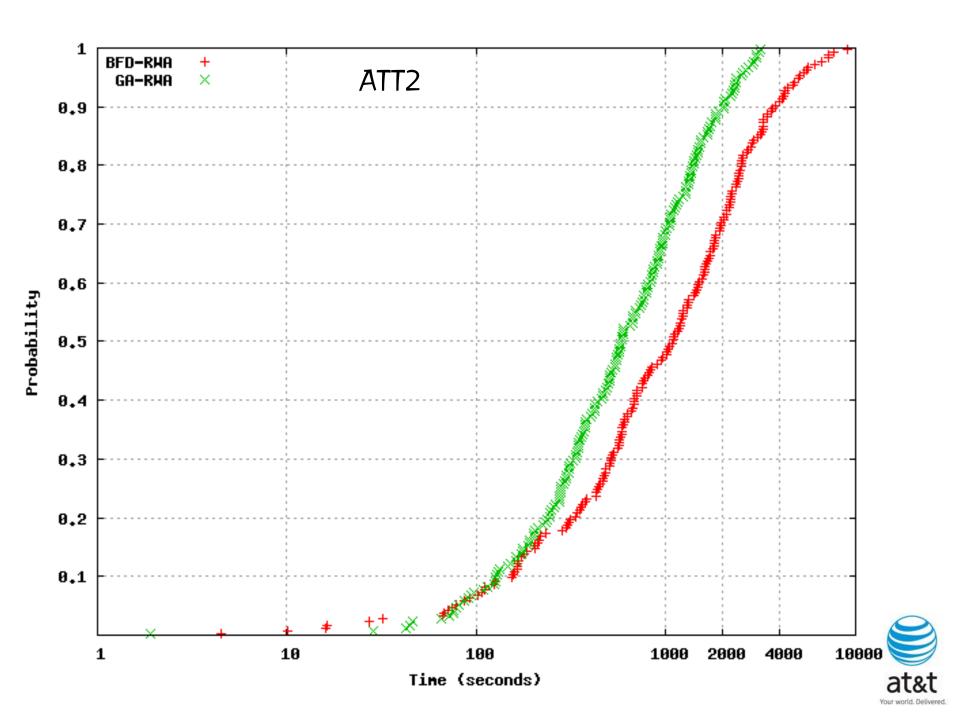














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- BRKGA heuristics are highly parallelizable. Calls to decoder are independent.

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- We have had only a small glimpse at BRKGA applications to problems arising in telecommunications.
- The BRKGAs described in this talk are all state-of-the-art heuristics for these applications
- We are currently working on a number of other applications in telecommunications, including the degree-constrained and the capacitated spanning tree problems and a metropolitan network design problem.





Thanks!

These slides and all of the papers cited in this talk can be downloaded from my homepage:

http://www.research.att.com/~mgcr

